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New Product Development by
Overcoming Complexity Constraints

SPYROS VASSILAKIS

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by Overcoming Complexity Constraints**

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Accelerating new product development by overcoming complexity constraints

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Abstract

The economic theory of technological change is a theory of investment. Agents invest in an activity called research; a black box process returns a value for a variable that shifts the production function. This paper proposes a way to open the black box. It is motivated both by theoretical arguments for opening this box, and by recent empirical literature on new product development that stresses the importance of nontraditional factors in determining firm performance. An example of the former is Solow (1994, p. 52): "... the production of new technology may not be a simple matter of inputs and outputs. I do not doubt that high financial returns to successful innovation will divert resources into R&D. The hard part is to model what happens then". An example of the latter is Baily and Gersbach (1995, p. 347), who discuss the determinants of operating efficiency of firms "Traditional determinants, such as capital intensity and scale were found to play a role. But innovations such as design for manufacturing and workplace organization turned out to be even more important".

This paper considers technological change, and in particular new product and process development, from a new perspective, that of complex problem-solving. Technological change is made possible by organizational techniques that reduce the complexity of problem-solving; differences in the technological performance of firms are attributed to their different problem-solving styles.

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(continuation of abstract)

More specifically, this paper proposes the formalism of constraint satisfaction problems (CSP) as (a) expressive enough to capture design problems, including design for manufacturing, listening to the voice of the customer, and robust design; and (b) tractable enough to be fully decidable, i.e. to possess an algorithm that will always correctly generate a solution, or the set of all solutions. This algorithm produces too much rework; in fact, rework is the main reason and symptom of slow new product development, both on theoretical and empirical grounds. To minimize rework, this paper proposes three distinct techniques. A technique to order decisions; a technique to make more specific the goals of design by communication prior to decision-making; and a problem-partitioning technique that minimizes subproblem size subject to the constraint of not creating extra extendability or coordination problems. The three techniques together probably minimize rework and thus accelerate decision-making.

The problem-partitioning technique in particular associates with each design problem a tree of subproblems; the size of the largest subproblem is an index of the degree of difficulty of the design problem. The nature of the technical and marketing constraints faced by product designers determines both the organizational form (the tree of subproblems) appropriate for the design problem and the speed of reaching a solution (an exponential term whose exponent is the size of the largest subproblem). This organizational form is reusable because it depends only on structural information, i.e. on which variables enter which constraints, not on the values that satisfy each constraint. The cost of building this organizational form is quadratic in the size of the design problem, i.e. other things being equal, larger firms with many interdependent products face disproportionately larger costs of adjusting their organizational forms to changes in the underlying structural information. If the underlying structure remains the same, though, an incumbent firm that has already computed its organizational form can amortize it over many different NPD efforts, and will develop new products faster than a new entrant who still has to figure out how to organize for new product development.

The empirical literature on new product development stresses the importance of design in determining operational efficiency. The empirical literature by itself, however, cannot pinpoint exactly how fast product developers differ from slow product developers; a result of this is that it is not clear to slow developers what they should be imitating to become fast product developers. Ward et al. (1995) make this point clearly in their discussion of Toyota's NPD organization, which they call set-based concurrent engineering: "We do not know enough about how set-based concurrent engineering is or should be performed.

Toyota's approach is not well-defined or documented", and "Since there is no proven formal methodology, learning the process will be slow and error-prone".

Furthermore, the empirical literature has not established causal relationships between time and problem-solving techniques; only associations have been documented. Ward et al. (1995) state "Each advantage of set-based concurrent engineering described earlier represents a hypothesis - that there is a causal relationship between Toyota's success and its use of set-based concurrent engineering. An important task for further research is therefore to demonstrate this causal link more carefully. Unfortunately such causes are difficult to show in complex organizations". Seen in this light, this paper contributes a well-defined set of techniques that provably accelerate NPD; these techniques could, therefore, provide a starting point for filling this gap in the literature.

1. Introduction

The economic theory of technological change is a theory of investment. Agents invest in an activity called research; a black-box process returns a value for a variable that shifts the production function. Economic analysis focuses on the appropriability of the returns to investment in research, i.e. on reasons why the social returns to investment in research might differ from private returns, and on policy measures designed to bring them closer together. This line of research was initiated by Nelson (1959) and Arrow (1962). It is also the theory underlying models of endogenous growth.

The investment/appropriability perspective is valuable; a lot of progress has been made exploring its implications in models where the divergence between private and social returns is generated by spillovers, imperfect competition, public goods, or asymmetric information. It is also clear from the literature that more is involved in the determination of technological change. Solow (1994, p. 52) states: "... the 'production' of new technology may not be a simple matter of inputs and outputs. I do not doubt that high financial returns to successful innovation will divert resources into R&D. The hard part is to model what happens then".

Rosenberg (1989) expands on this point: "The critical factor for commercially successful innovation, however, may well be the utilization of the results of R&D. The market-failure analysis must be supplemented by an analysis of the conditions affecting the utilization of the results of R&D. Utilization of the results of research is heavily influenced by the structure and organization of the research system within an economy, a topic on which the neoclassical theory is either silent or incorrect". Romer (1994, pp. 9-21) reaches similar conclusions,

and Solow (1994, p. 53) concludes his survey of Growth Theory: "...I think the best candidate for a research agenda right now would be an attempt to extract a few workable hypotheses from the variegated mass of case studies, business histories, interviews, expert testimony, anything that might throw light on good ways to model the flow of productivity - increasing innovations and improvements".

New product development (NPD) is a good place to start taking Solow's advice. There is a growing empirical literature on it that does offer a few workable hypotheses to start with: Clark and Fujimoto (1991), Wheelwright and Clark (1992), Clausing (1994), Ulrich and Eppinger (1995). This literature emphasizes, concurrent product and process development; I will discuss both under the NPD heading. The mathematical model introduced in this paper is directly motivated by it; I will spend some time describing its main points.

The first point is that most NPD involves application of already existing widespread knowledge, not a scientific breakthrough or any significant new learning. Gomory (1989) states: "There is another process of innovation, which is far more critical to commercializing technology profitably. Its hallmark is incremental improvement, not breakthrough. It requires turning products over again and again; getting the new model out, starting work on an even newer one. There is no brand new product here, no revolutionary technology.... It is competition among ordinary engineers in bringing established products to market". I will concentrate on such routine NPD and I will call mature the industries with a well-established stock of relevant scientific and technological principles known to all firms in the industry. The automobile industry is an example.

The second point is that in mature industries NPD cannot deliver long-lasting monopoly positions. The critical performance variables are, instead, the cost, variety, quality and time-to-market of the new products. All sources agree on this so I will just refer to Blackburn (1991, Ch. 5), Stalk and Hout (1990, Ch. 4) and Womack et al. (1989, Ch. 5). The ability to develop new products faster than competitors do, in particular, has a number of strategic advantages. Demand and technology change in unpredictable ways; fast NPD reduces the risk of coming up with a product no longer in demand. Graham (1986) for example, describes the development of the Selectavision video disc by RCA; it took 15 years of work, and when it was introduced in 1981, "... as the expected generator of \$7.5 billion in annual retail sales by 1990, it was the legitimate hope for the future of all RCA" (Graham, 1986, p. 26). Instead, videodisc production was discontinued in 1984, RCA lost 580 million USD, and soon after ceased being an independent company. RCA managers explained the failure in the following terms. "Our mistake was we were late. Five years earlier it would have been a

huge success, three years earlier it would have been a good success.” (ibid., p. 217). The videodisc lost to the then new VCR. Similar cases are described in Stalk and Hout (1990, Chs. 2 and 4). Note that the strategic advantage of fast NPD does not depend on customers’ preferences for wide variety or frequent model upgrades. Womack, et al (1989, p. 127) make the point. “The producers in full command of these techniques can use the same development budget to offer a wider range of products or shorter model cycles — or they can spend the money they save by implementing an efficient development process for developing new technologies. And in every case, the shorter development cycle will make them more responsive to sudden changes in demand. The choice, and the advantage, will always lie with lean producers.”

The third point is that some firms seem to be systematically faster in developing new products; and that their speed advantage cannot be reasonably attributed to extra effort, better engineers, more computing power, less complex products, or chance. In fact, the most surprising result of the Clark and Fujimoto (1991) and Womack et al (1989, Ch. 5) studies was that the faster product developers were also those using significantly less engineering effort, even after adjusting for differences in the products developed. The companies studied were all world-class, with open access to the best available resources. In fact, Clausing (1994, p. 5) emphasizes that there are no significant differences in the quality of engineers in the countries covered by the studies (US, Japan, Germany). The fastest product developers (Honda, Toyota) have since demonstrated, by designing products outside their home markets (Florida, (1993, p. 121)) that their speed advantage is not related to regional differences; and wide firm differences within each region (Toyota and Nissan are frequently cited) have reinforced this point. Furthermore, the speed advantage of the fastest product developers was not achieved by sacrificing low production cost or high product quality. In fact, Honda and Toyota are pioneers of quality function deployment (QFD), design for manufacturing, and robust design, techniques that accelerate design of new products taking into account quality and cost targets. Finally, faster product developers were not merely luckier product developers. They have repeated their success across time and across different markets. They use distinctly different NPD techniques; when these techniques were adopted by other firms (Clausing (1994, p. 47) cites Ford and Xerox as “early outstanding successes”) development time was drastically reduced.

The fourth point reinforces the third. There was a large difference in the initial condition, of Honda or Toyota on the one hand, and Ford and GM on the other. In the early ‘50’s, Toyota produced in a year what GM produced in a day. Ford was the firm that made automobiles affordable by introducing mass production techniques. GM was the ideal company, managed so effectively it had been able to overtake Ford by offering larger variety and an annual model change

at affordable prices. These two firms were the repositories of all knowledge on mass-production automobile manufacturing and management; others learned about automobiles either through publicly available channels (engineering textbooks) or by visiting Detroit. (In such a visit, T. Ohno, later Toyota's chief engineer, estimated that Detroit firms had a 10-to-1 productivity advantage over Toyota; see Ohno (1988, p.68). According to the investment/appropriability theories of technological change, their larger volume should have provided Detroit firms with the advantages of scale economies and learning-by-doing; drawing from the same labor market should have provided the advantages of technological spillovers and of cross-pollination of ideas; recruiting from the top universities in the world should have provided the advantages of human capital; and outspending their rivals in R&D, and having a larger stock of knowledge to begin with, should have provided the advantages of accumulated knowledge capital. Despite these accumulated advantages, Detroit firms lost market share to firms (like Toyota and Honda) that were able to offer simultaneously lower cost, higher quality, more variety and faster model replacement. Womack et al (1989) document this story and provide the following example as an illustration of the fact that faster product development is not due to the "usual suspects" of more knowledge or more capital. They describe how Toyota in the '70's redesigned 4-cylinder engines to maximize their power, and in the process changed its image among consumers from a "low-tech weakling" to a "high-tech wonder". They conclude (ibid., p. 132) "This perception on the part of consumers was enormously frustrating to engineers in many of the mass-production companies who knew that all these "innovations" had been around the motor industry for decades . . . What's more, when they tried to copy these "innovations" on a wide scale, the weaknesses of their engineering systems were exposed. In many cases it took years to introduce a comparable feature, and often it was accompanied by drivability problems or high production costs. GM, for example, lagged Toyota by four years in introducing many of the features we just listed in its Quad Four engine; it needed two more years to teach a high level of refinement." (Womack, et al. (1989, p. 116)).

The fifth point is that NPD is a problem-solving activity. In particular, NPD is not merely a special case of the theory of investment under uncertainty. Wheelwright and Clark (1992, p. 218) state "... in the final analysis, when we search for an understanding of truly outstanding development, we must eventually get down to the working level where individual designers, marketers and engineers work together to make detailed decisions and solve specific problems. The magic of an outstanding product is in the details. Thus, detailed problem solving is at the core of outstanding development".

The sixth point is that NPD is a complex problem-solving activity. In Clausing's (1994, p. 57) words, "in developing a complex product, there may be

10 million decisions. Although individuals can make most decisions, the most critical decisions (roughly 1,000 to 10,000 for large, complex products) require more attention, and most of them do not lie entirely within the experience of any individual or group." Ulrich and Eppinger (1995, p. 4) state that "... very few products can be developed in less than a year, many require three to five years, and some take as long as ten years." Developing the Chrysler Concorde car, for example, requires the design of 10,000 unique (to this car) parts, 2,250 people, 3.5 years and one billion dollars (*ibid.*, p. 6). Clark and Fujimoto (1991, p. 73) find that, on average, a new car design takes 2.5 million engineering hours, spent over a period of 54 months.

The seventh point is that fast and slow developers differ in their approach to solving complex problems; and that this shows up in the amount of rework (iteration, backtracking, design revision) they generate. Slow developers divide a NPD problem into sub-problems functionally, i.e. using the technical nature of the decisions as a dividing criterion. For example, all customer-related decisions like styling and features are made by marketing; all product engineering-related decisions are made by design; and all process engineering decisions are made by manufacturing. Slow developers typically order their decisions sequentially. Technology-driven firms start with the decisions that produce a technically feasible, functioning product, and worry about manufacturability and customer appeal later; styling-driven firms start with the decisions that produce an attractive product, and worry about technical feasibility later. Finally slow developers limit communication between sub-problems to occur when a functional group delivers a complete design, or a request for a change in a complete design, to another such group; this is usually called "throwing the design over the wall" to another group.

A typical result of such a process is that the first functioning design is too costly to make, so manufacturing returns the design to engineering for rework; or that the first functioning design does not appeal to customers, so marketing returns the design to engineering for rework. Changes to accommodate manufacturing are typically not consistent with those that please marketing, so further rework typically occurs. Fast product developers, on the contrary, use the degree of interaction among decisions, not membership in a skill category, as the criterion of assigning decisions into sub-problems. If a marketing decision like car height interacts with an engineering decision like engine power (and therefore size), then these decisions must belong to the same sub-problem, even if they belong to different functional specialities. Sub-problems are usually identified with teams, because each sub-problem is the responsibility of a dedicated team. In Clausing's (1994, p. 40) word, "Many critical interfaces have a dedicated team. Teams are formed wherever they are needed to achieve an integrated approach to the development of the new product. The formation of the

best interlocking structure of teams is a key success factor." This is the subject of parts 5 and 6 of this paper.

Problem partitioning is made necessary by complexity; incorrectly done, it generates rework. Similarly, complexity dictates that decisions have to be made one at a time, due to working memory limitations. The order of making decisions matters. Earlier decisions constrain later ones, thus reducing search effort; but earlier decisions could constrain later ones by eliminating the desirable options, thus generating rework. Two of the "cash drains of traditional product development" described by Clausing (1994, pp. 19–20) are examples of incorrect ordering of decisions. They are "technology push" (clever technology is developed that does not satisfy any significant customer need); and "disregard for the voice of the customer". Clausing (1994, p. 20) states "The first step in the development of a specific new product is the determination of the customer's needs. In traditional product development the product has often been doomed to mediocrity before the completion of the needs activity. The biggest culprit has been the deployment of the voices of corporate specialists, rather than the voice of the customer". Fast developers, instead of starting with how to make a technically satisfactory, functioning product, start with making decisions on the values of the variables that are directly relevant to customers. This is usually called concept generation and selection. See Ulrich and Eppinger (1995, p. 79, exhibit 2). Technical considerations are used at this stage to guide the concept generation and selection process, not to make technical decisions. The ordering of decisions is considered in part 3 of this paper.

The need for communication in NPD is also dictated by complexity. Decisions made in different sub-problems have to be checked for consistency; and earlier decisions have to be checked for consistency with later decisions. Lack of consistency implies revision of already made decisions, i.e. rework. Slow developers are characterized by infrequent communication between decision-makers, relatively late in the NPD process. Fast developers are characterized by a large amount of communication early in the NPD process. Womack et al. (1989, p. 115) state "In the best team projects, the numbers of people involved are highest at the very outset. As development proceeds, the number of people involved drops as some specialities are no longer needed. By contrast, in many mass-production design exercises, the number of people involved is very small at the outset but grows to a peak very close to the time of launch, as hundreds or even thousands of extra bodies are brought in to resolve problems that should have been cleared up in the beginning." Communication in slow NPD groups takes place after design decisions have been made on a large part of the product; these decisions are "thrown over the wall" to a group responsible for another set of decisions. Communication in fast NPD groups takes place before, as well as after, design decisions have been made. Communication before decision-making

does not intend to render already taken decisions consistent; but to render more concrete the goals of NPD by eliminating values of variables that are not consistent with any values of other variables, and thus avoid rework in the future. For example, the goal of achieving durability of a part may be achieved by gold-plating it; if this is consistent with none of the allowed values of the total cost variable, the gold-plating option can be eliminated before design begins: gold-plating could never be part of an acceptable design. Ulrich and Eppinger (1995, p. 93) classify this kind of communication in their concept generation phase of NPD (they give an example of excluding from the beginning the nuclear power option for supplying with energy a hand-held nailer, even though the design team knew of nuclear devices used to power artificial hearts). This paper discusses communication in section 4.

The literature cited suggests that rework is the characteristic symptom of slow NPD; and that what makes the difference between fast and slow product developers is their problem-partitioning, decision-ordering, and communication techniques. The present paper presents a causal relation between such techniques and the amount of rework; it is organized as follows.

Part 2 will define product development as a constraint satisfaction problem (CSP), and will show that constraint satisfaction problems are sufficiently expressive to capture the concerns of product developers (listening to the voice of the customer, design for manufacturing, robust design, . . .). Part 3 will present the main algorithm for solving constraint satisfaction problems, and will explain why it generates rework. Part 4 will present a special class of constraint satisfaction problems (binary, tree-structured ones) for which a decision-ordering technique and a communication technique are sufficient to eliminate rework (no problem partitioning is needed).

Parts 5 and 6 consider arbitrary CSP's and their transformation into binary, tree-structured CSP's. This transformation depends on a particular problem partitioning method. Part 5 considers the properties of each individual subproblem. Part 6 explains how the subproblems are linked to each other to form a tree; and how this tree is used to transform the original CSP into a binary tree-structured one, so that the methods of section 4 can be applied to eliminate rework between subproblems. Part 7 discusses the costs and benefits of these methods. Part 8 concludes.

2. Design problems as constraint satisfaction problems

To define the design problem mathematically, I will first borrow a description of the design problem from the literature on "quality function

deployment"; see Hauser and Clausing (1988), Wheelwright and Clark (1992, p. 229), and Clausing (1994). Suppose that the design task is the development of a gear system for the automatic film rewinder of a camera. The consumer of a camera cares about some of its attributes: speed of rewinding, sound, reliability, cost, size,.... Each of these attributes can be represented by a variable that takes values in some finite domain. The values of the variables are restricted by consistency constraints: for example, a camera of some size and reliability cannot cost less than some amount. To deliver the attributes valued by the customer, engineers have to decide on a number of engineering attributes: number of gears, diameter of gears, number of teeth per gear,.... Engineering attributes can also be represented by variables that take values in some finite domain. There are also consistency constraints between engineering and customer attributes: for example two gears of a certain size and tooth profile cannot generate a sound lower than some level. Finally, there are consistency constraints between the engineering attributes themselves: for example, the weight and size of gears are related. In a similar way, one can link engineering attributes to production process attributes, and therefore to cost, quality and variety attributes. Finally, the objectives of design can also be represented by a relation (a constraint) between attributes: for example, deliver a rewind system that costs less than a certain amount, rewinds in less than a certain amount of time, and will not break down before it is used a certain number of times. In the words of Chandrashekar (1990, p. 65): "Formally, all design can be thought of as constraint satisfaction".

The considerations of section 1 motivate the study of the following problem

Definition 1: A constraint satisfaction problem (CSP) is a tuple $\langle X, D, R, s, e \rangle$

- $X = \{x_1, \dots, x_n\}$ is a finite set of variables;
- $D = \langle D_1 \dots D_n \rangle$ is a tuple of finite sets;
 D_i is the domain of variable x_i .
- R is a tuple of relations (constraints). Each relation $c \in R$ is defined by its scope $s(c) \subseteq X$, i.e. the variables it involves, and its extent $e(c) \subseteq \prod_{i \in s(c)} D_i$, i.e. the tuples that satisfy c .

Definition 2: A solution of a CSP $\langle X, D, R, s, e \rangle$ is a tuple $u = \langle u_1 \dots u_n \rangle$ such that

- $u_i \in D_i$ for all $i = 1, \dots, n$

- for each constraint $c \in R$ with $\text{scope}(c) = \{x_{i_1} \dots x_{i_k}\}$, we have $(u_{i_1}, \dots, u_{i_k}) \in e(c)$, i.e. all constraints are satisfied by u .

This formulation of the product design problem is sufficiently expressive to capture not only the basics, but also design for manufacturing, and robust design. Design for manufacturing takes into account manufacturing cost at the time the product is designed; seemingly minor design details can have a major impact on cost. For example, there is usually some room to vary the number of components that make up a product, and a number of options as to how the components will be attached to each other. More components imply less fabrication cost but greater assembly cost; using screws to attach components to each other increases assembly time, but facilitates product disassembly for repair and maintenance. These concerns can be captured in a CSP by introducing extra variables for the number of components of the product, and for the method of attachment; and extra constraints to capture the relations between the values of these extra variables and other variables appearing in the CSP (e.g. Cost). Design for manufacturing is discussed in Whitney (1988), and Ulrich and Eppinger (1995, Ch. 9) and their references. Robust design takes into account the fact that product performance is conditional on the values of variables not controlled by the customer; it aims to deliver the same product performance over a wide range of the values of these variables, i.e. to deliver “robust quality” (Taguchi and Clausing (1990)). This increases the value of the product to the customer and, according to Clausing (1994, p 74), “robustness also greatly shortens development time by eliminating much of the rework that is known as build, test and fix.” An example of the kind of variables that affect product performance but are not under customer control is given by Clausing (1994, p. 75) “A lemon is a car that has excessive production variations. To overcome this, the production process has to be robust so that they produce less variation, and the car design has to be more robust so that its performance is less sensitive to production variations. The customers also want a car that will start readily in winter and not overheat during the summer; that is, they want a car that is robust with respect to the variations of customer use conditions.” Robustness considerations can be expressed by a CSP if each variable is replaced by a set of variables, each of which expresses the same attribute in a different state of nature. Robustness is imposed by requiring that all these variables take the same value, i.e. by extra constraints. Still more constraints can express the relation of attributes in different states of nature.

The finiteness of the domains of a CSP ensures that we can always decide whether a given CSP has a solution or not. The method is called generate and test (GT): for each tuple u in ΠD_i , test if each constraint c in R is satisfied. If yes, declare a solution. If no, generate another tuple u and test it. There are only finitely many tuples in ΠD_i , so GT will eventually terminate. GT is obviously

grossly inefficient, and we cannot expect to solve any CSP of reasonable size using it. Formally, the number of steps GT takes to compute all solutions to a CSP is an exponential function of the number of variables in the problem (Mackworth (1992), p. 6). Perhaps surprisingly, it is not known whether there exists or not an algorithm that solves the CSP in a number of steps that is a polynomial function of the number of variables ("in polynomial time"). What is known is that if such an algorithm exists, then many other combinatorial problems will have such an algorithm (CSP is NP-complete). Such problems are widely believed to be intractable, i.e. not solvable by an algorithm in polynomial time. For solving such problems, therefore, it is imperative to have good structuring techniques (problem-partitioning and solution-integration techniques) that reduce the complexity of problem-solving, search techniques more efficient than generate-and-test, and "decision-ordering" and "communication" techniques that reduce the amount of rework.

3. Rework

Generate-and-test is inefficient because it first generates a complete vector of values u_1, \dots, u_n and then checks for consistency. If inconsistency between, say, u_2 and u_3 could be detected before u_4 is generated, then we would not need to check the whole vector for consistency (nor expand it beyond u_4). This idea is captured by depth-first search of the search-tree generated by the CSP in question.

Definition 3.1: Let $\langle X, D, R, s, e \rangle$ be a CSP. Order $X = \{x_1 \dots x_n\}$ and each domain D_i in an arbitrary way. The search tree generated by $\langle X, D, R, s, e \rangle$ is defined to be a rooted tree; the children of the root are the elements of D_1 in ascending order; they are called first-level nodes. The children of any i -th level node, $1 \leq i \leq n-1$, are the elements of D_{i+1} in ascending order. Level n nodes are leaves, i.e. have no children. A path from the root to a leaf is a complete assignment (of values to variables). A path from the root to an internal node at level i is a partial assignment up to level i .

Definition 3.2: A partial assignment up to level i is consistent if it satisfies all the constraints whose scope is a subset of $\{x_1, x_2, \dots, x_i\}$.

Assignments, partial or complete, can be thought of as analytical prototypes. Ulrich and Eppinger (1995, p. 219) define a prototype "as an approximation of the product along one or more dimensions of interest.

Analytical prototypes represent the product in a non tangible, usually mathematical, manner". The backtracking (BT) algorithm builds an analytical prototype gradually, by successively assigning values to variables and checking for consistency.

When no variable has been assigned a value, the algorithm is at level 0 (at the root of the search tree). The algorithm starts by assigning to x_1 , the first variable in x , its first value; it is then at level 1. Suppose that the algorithm has built up a partial assignment $u_1 u_2 \dots u_k$ up to level $k, 1 \leq k \leq n$. If $k=n$, the algorithm terminates with success. If $k < n$, the algorithm picks the first value u_{k+1} in D_{k+1} consistent with $u_1 \dots u_k$; and extends the assignment by setting $x_{k+1} = u_{k+1}$. If no such value of x_{k+1} exists, the algorithm destroys the assignment $x_k = u_k$, i.e. it backtracks to level $k-1$; and creates the assignment $x_k =$ successor of u_k , thus returning to level k . If u_k has no successor (because it is the last element of the domain of x_k), the algorithm backtracks to level $k-2$ by destroying the assignment $x_{k-1} = u_{k-1}$ as well; it then returns to level $k-1$ by setting $x_{k-1} =$ successor of u_{k-1} ; and it checks this assignment for consistency with values in D_k . If the algorithm backtracks to level zero, and u_1 has no successors, then the algorithm terminates with failure.

The BT algorithm will always terminate, since it traverses a finite search tree (depth-first). It is sound, in the sense that if it terminates with success, then the complete assignment associated with successful termination is in fact a solution of the CSP by construction; and if it terminates with failure, the CSP has in fact no solution, since all branches of the search tree have been examined without finding a solution. It is complete in the sense that if the CSP has a solution, the algorithm will terminate with success; and if the CSP has no solution, the algorithm will terminate with failure. These properties, together with its superiority over the generate-and-test algorithm, motivate its use.

The BT algorithm generates rework every time it backtracks; a previously made decision is changed, and additional constraint checks take place. What is the importance of rework in determining development time? To see this, let $r = |R|$ be the number of constraints, and $K = \max_i |D_i|$ the number of values in the largest domain. A solution obtained without rework requires at most rKn constraint checks. (The BT algorithm in this case never encounters a non-extendable partial assignment. At each level it checks at most K values of x_{t+1} for consistency with the existing assignment up to level t . There are r constraints, so at each level at most rK checks take place. And there are n levels, so at most rKn checks take place overall.) A solution in general, however, can require up to rK^n constraint

checks. This is because in the worst possible case, all K^n possible complete assignments will have to submit to at most r consistency checks each. The difference $rK^n - rKn$ is due entirely to rework, and is huge even for moderate values of n ; for $r=1$, $K=2$, $n=54$, and assuming a million constraint checks per second, the difference is a thousand years. Minimization of rework is thus practically equivalent to minimization of total development time. The three techniques introduced later on reduce the “effective” K , n and r respectively. The communication technique reduces the size of the domains by eliminating options. The problem partitioning technique reduces the number of variables. The decision-ordering technique reduces the number of constraint checks. I start with an important special case.

4. Binary, tree-structured constraint satisfaction problems

A CSP is binary if the scope of each constraint contains at most two variables. is tree-structured if its primal graph is a tree, i.e. a connected, acyclic graph.

Definition 4.1: The primal graph of a binary CSP $\langle X, D, R, s, e \rangle$ has X as its node set; and there is an edge (x, y) in the primal graph if and only if there is a constraint in R with scope $\{x, y\}$.

The main result in this section is that a decision-ordering and a communication technique applied to a binary, tree-structured CSP, allow the BT algorithm to find a solution without rework. The two techniques themselves are easy to apply, in a well-defined sense. The next example illustrates the importance of a correct ordering of the variables.

Example 4.1: Consider the CSP problem with $X=\{x_1, x_2, x_3\}$, $D_i=\{0,1\}$, $R=\{c_{12}, c_{23}\}$, $s(c_{ij})=\{x_i, x_j\}$, $e(c_{12})=\{00, 11\}$, $e(c_{23})=\{01, 10\}$. Its primal graph is a tree. Consider first what happens if the variables are searched in the order $x_1-x_3-x_2$. The BT algorithm first sets $x_1=0, x_3=0$ (there are no constraints linking x_1 to x_3). It then performs the constraint checks $c_{12}(0,0)$, $c_{23}(0,0)$, $c_{12}(0,1)$, and discovers that $x_1=0, x_3=0$ is not consistent with any value of x_2 . Hence it backtracks, sets $x_3=1$, and performs the constraint checks $c_{12}(0,0)$, $c_{23}(0,1)$, both successful. In the ordering x_1, x_2, x_3 , however the assignment $x_1=0$ is immediately followed by the constraint check $c_{12}(0,0)$, since x_1 and x_2 are linked by a constraint. This being successful, the BT algorithm performs the test $c_{23}(0,0)$, which fails. It then tests $c_{23}(0,1)$, which succeeds. Hence, in the ordering $x_1-x_3-x_2$ a solution was found with five constraint checks, while in the ordering $x_1-x_2-x_3$, with only three.

Note that in the ordering $x_1-x_3-x_2$, x_2 is linked by an edge to two of the variables preceding it, forcing two constraint checks of each extension of a partial assignment that requires checking. In the ordering $x_1-x_2-x_3$, however, each variable is linked by an edge to at most one variable preceding it, so that pruning of the search tree is more gradual and starts earlier than in the ordering $x_1-x_3-x_2$; in the latter, no constraint limits that (x_1, x_3) assignments, and all pruning takes place when all but one variable have been assigned values, thus negating the advantage of backtracking over generate-and test. This motivates

Definition 4.2: A total order $<$ on the nodes of a graph has width one if for each node u there is at most one $v < u$ such that (u, v) or (v, u) is an edge of the graph.

The nodes of a tree can be ordered with a width-one ordering in time proportional to the number of nodes in the tree. One way to construct such an ordering is to pick a node and designate it as the root of the tree; then rank its successors; then rank the successors of its successors, . . ., until the children of all nodes are ranked. Then visit the nodes depth-first, starting from the root, and from the first child of each node. Define $u < v$ if u is visited before v ; $<$ is a total order.

Fact 4.1: The ordering on the nodes of a tree generated by depth-first search if of width one.

Proof: Suppose, for contradiction, that this ordering is not of width one. Then there is a node u that is linked by tree edges (u, v_1) and (u, v_2) to two of its predecessors in the ordering generated by depth-first search of the tree. Since $<$ is a total order, assume without loss of generality that $v_1 < v_2 < u$, i.e. v_1 is visited before v_2 , and v_2 before u . Since $v_1 < u$ and (v_1, u) is an edge of the tree, depth first search will visit it immediately after it visits all the children of v_1 ranked before u . Since $v_1 < v_2 < u$, v_2 must be a child of v_1 ranked before u , or a descendant of such a child. In either case, there is a tree edge (v_1, w_1) , with w_1 ranked before u , and tree edges (w_1, w_2) (w_2, w_3) . . . (w_{k-1}, w_k) with $w_k = v_2$, $k \geq 1$. But then the tree contains the path $(u, v_1)(v_1, w_1) \dots (w_{k-1}, w_k)(w_k, v_2)(v_2, u)$, i.e. a cycle, while trees are acyclic.

This decision-ordering technique is designed to reduce the number of constraint checks needed to find a solution. The communication technique I discuss next aims to reduce the size of the domains before search begins by eliminating the “gold-plating” options discussed in the introduction; formally it aims to achieve directed arc consistency (DAC), a property I define next.

Definition 4.3: (Dechter and Pearl (1989)) Let B be a binary, tree-structured CSP with a width-one ordering of its variables. B is directionally arc consistent if

for any constraint c with scope $\{x_i, x_j\}$ and $x_i < x_j$, every value a in D_i is supported by some value b in D_j , i.e. (a, b) belong to the extent of constraint c .

The next fact shows why Definitions 4.2 and 4.3 are interesting.

Fact 4.2: Let B be a binary, tree-structured, width-one ordered, directionally arc consistent CSP. Then the BT algorithm will find a solution without rework.

Proof: Rework occurs only at a dead-end, i.e. when a partial assignment $v_1 \dots v_i$ cannot be consistently extended to the next variable. I show by induction on i that a dead-end can never occur. For $i=1$, this is guaranteed by DAC. For general i , the assignment $v_1 \dots v_i$ already satisfies all constraints with scopes in the set $\{x_1, \dots, x_i\}$, by definition of the BT algorithm. There is at most one constraint with scope containing x_{i+1} and some x_j , $1 \leq j < i$ (width - one ordering guarantees this); call this constraint $c_{j,i+1}$. By DAC there is a value v_{i+1} in D_{i+1} that supports v_j , hence $v_1 \dots v_i v_{i+1}$ is a consistent extension of $v_1 \dots v_i$, and no rework will ever take place.

The next fact states that cost of solving a CSP without rework.

Fact 4.3: Let B be a binary, tree-structured, width-one ordered, directionally arc consistent CSP. The BT algorithm will find a solution of B after at most nk constraint checks (k is the size of the largest domain of B).

Proof: The search tree has n levels. By fact 4.2, the BT algorithm will proceed from one level to the next without rework. At each level, there is at most one j such that $(j, i+1)$ is the scope of some constraint. Hence v_j needs to be tested for consistency with some value in D_{i+1} at most k times (until its support in D_{i+1} is found). Hence, at most nk constraint checks will be performed.

These three facts suggest the following strategy for solving a binary, tree-structured CSP; (a) compute a width-one ordering of its variables; (b) make B directionally arc consistent; and (c) find a solution using the BT algorithm. It remains to be seen how task (b) is done; the algorithm that makes B DAC is our communication technique. I present it in two steps. Suppose first that there is an algorithm g that takes as inputs pairs of domains (D_i, D_j) and outputs the set of elements of D_j that are supported by some element of D_i ; if there is no constraint whose scope is the set $\{x_i, x_j\}$, g outputs D_j . The algorithm, call it C , that achieves DAC uses g as a subroutine. It works on a binary, tree-structured, width-one ordered CSP as follows. Start with the last variable x_n in the width-one ordering. Find its parent, i.e. the unique variable preceding it in this ordering and linked to

it by an edge of the primal graph. (Each variable has a unique parent because the primal graph is a tree and the ordering is width-one.) Replace $D_{\text{parent}(n)}$ by $g(D_n, D_{\text{parent}(n)})$, i.e. eliminate from the domain of $\text{parent}(n)$ all those values not supported by some value in D_n . Repeat for $x_{n-1}, x_{n-2}, \dots, x_2$.

Fact 4.4: Algorithm C transforms a binary, tree-structured width-one ordered CSP B into an equivalent CSP B' with the DAC property.

Proof: Let c be a constraint in R with scope $\{x_i, x_j\}$ and $x_i < x_j$. Let a be a value in D'_i , the domain of x_i generated by the C algorithm. I show that a has support in D'_j . First note that x_i is the parent of x_j in the width-one ordering. Hence, at step j of the C algorithm, all values in the domain of x_i without support in the domain of x_j are eliminated. The domain of x_i can only shrink or remain the same after step j , hence all its values when C terminates have support in the domain of x_j , since the latter never changes after step j of algorithm C.

Algorithm C uses subroutine g ; the latter can be described as follows. It starts with the domains of two variables, D_i and D_j , that are linked by a constraint. It takes the first value in D_j , and checks whether there is a value in D_i that supports it; this step takes at most $|D_i|$ constraint checks. If the answer is yes, it declares this value supported, and proceeds to the second value of D_j . If the answer is no, it deletes this value from D_j and proceeds to its second value. It repeats until all the values of D_j have been either deleted or declared to be supported.

Algorithms C and g are in fact communication techniques; at each step j of g , someone responsible for decision x_j asks someone responsible for decision $x_{\text{parent}(j)}$ whether $x_j=a$ is consistent with some value of $x_{\text{parent}(j)}$. The answers are then codified by algorithm C, which deletes unsupported values. How costly is communication? This is answered by

Fact 4.5: A binary, tree-structured, width-one ordered CSP can be turned into a DAC CSP with at most nk^2 constraint checks.

Proof: Algorithm C goes through n stages; at each stage i it runs the subroutine $g(D_i, D_{\text{parent}(i)})$. Algorithm g checks each value of D_i for consistency with some value of $D_{\text{parent}(i)}$; at most k^2 such checks are needed to find support for every value of $D_{\text{parent}(i)}$ that has such support, and delete the rest.

Facts 4.1 to 4.5 show that the total cost of solving a binary, tree-structured CSP without rework is $n+nk+nk^2$. Note that no problem-partitioning technique is

needed to eliminate rework in this special case. In this sense, a binary, tree-structured CSP has optimal structure. The purpose of problem partitioning is to transform an arbitrary CSP into an equivalent binary, tree-structured CSP.

5. Problem partitioning

This section and the next deal with arbitrary CSP's. They show how arbitrary CSP's can be transformed into equivalent binary, tree-structured CSP's; so that the techniques of section 4 can be applied to obtain a solution without rework. The peculiar feature of the transformed CSP's is that their "variables" are subproblems of the original CSP; the domains of the "variables" are the solution sets of the corresponding subproblems; and all the constraints are binary, equality ones that enforce that each variable of the original CSP is assigned the same value in any two subproblems. Recall that in order to solve a CSP with n variables, r constraints, and domains containing up to k values, one may need up to rk^n constraint checks. Hence, any problem decomposition seems likely to generate large time savings, since $rk^{n_1} + rk^{n_2}$ is smaller than $rk^{n_1+n_2}$ when n_1 and n_2 are close to each other. Problem decomposition, however, creates two new problems, namely extendability and coordination.

A solution of a subproblem may not be extendable to a full solution; and the solutions of two subproblems may be extendable to full solutions, but not to the same full solution. This is illustrated by the following example.

Example 5.1: Consider the CSP defined by $X=\{x_1, x_2, x_3, x_4, x_5\}$, $D_i = \{\alpha, \beta, \gamma, \delta\}$, $R=\{c_{124}, c_{13}, c_{45}, c_{234}\}$, the obvious scopes, i.e. $s(c_{12})=\{x_1, x_2\}$, and extents given by $e(c_{124}) = \{\alpha\delta\delta, \beta\gamma\alpha, \gamma\beta\gamma, \delta\alpha\gamma\}$, $e(c_{13}) = \{\alpha\delta, \beta\gamma, \gamma\beta\}$, $e(c_{234}) = \{\delta\delta\delta, \gamma\gamma\alpha, \beta\beta\gamma, \alpha\alpha\gamma\}$, $e(c_{45}) = \{\delta\alpha, \beta\gamma, \alpha\delta\}$.

In what follows, I will represent each constraint by its scope, i.e. 12 will stand for c_{12} . The subproblem $\{124, 234\}$ has four solutions, namely $x_1x_2x_3x_4 = \alpha\delta\delta\delta, \beta\gamma\gamma\alpha, \gamma\beta\beta\gamma, \delta\alpha\alpha\gamma$. The subproblem $\{124, 13, 234\}$ is satisfied only by the first three of these. The original problem has two solutions, namely $x_1x_2x_3x_4x_5 = \alpha\delta\delta\delta\alpha, \beta\gamma\gamma\alpha\delta$. The partial solutions $\delta\alpha\alpha\gamma$ and $\gamma\beta\beta\gamma$ are not extendable to a full solution. The partial solution $\alpha\delta\delta\delta$ of $\{124, 234\}$ and the partial solution $\beta\gamma\gamma\alpha$ of $\{124, 23, 234\}$ are both extendable, but to different full solutions.

The example shows that arbitrary decompositions into subproblems will not eliminate rework. The basic tool for finding the right decomposition is the dual graph of a CSP; it records which constraints share which variables, i.e. the potential extendability and coordination problems. In the definition that follows, I use the notation $\langle V, E, \ell \rangle$ for a labelled graph; V is the set of nodes of the graph, $E \subseteq V \times V$ is its set of edges, and ℓ is a function that assigns a label to each edge.

Definition 5.1: The dual graph of a CSP $\langle X, D, R, s, e \rangle$ is defined by

- $V = R$
- $E = \{(c_1, c_2) \in R \times R : s(c_1) \cap s(c_2) \neq \emptyset\}$
- $\ell(c_1, c_2) = s(c_1) \cap s(c_2)$.

The dual graph of the CSP in ex. 5.1 has nodes 124, 13, 45, 234; edges (124, 13), (124, 234), (13, 234), (45, 234), (124, 45); and labels of edges (in the same order) 1, 24, 3, 4, 4.

I will only consider CSP's with connected dual graphs; otherwise, an efficient algorithm can find the connected components of the (disconnected) dual graph, and each of them can be solved separately. I will only consider CSP's with reduced dual graphs, i.e. CSP's in which no constraint's scope is a subset of another constraint's scope; otherwise, if $s(c) \subset s(c')$, c can be eliminated and $e(c')$ can be restricted to contain only tuples consistent with $e(c)$ on $s(c)$. In a CSP with reduced dual graph, each constraint is uniquely represented by its scope; I will adopt this notation from now on.

What is the best criterion for problem-partitioning? In ex. 5.1, consider the partitioning $\{124, 13\}$ and $\{234, 45\}$. The two subproblems have to communicate to set the values of x_2, x_3, x_4 consistently; that is why they are linked with edges (124, 234) and (13, 234), labelled with 24 and 3 respectively. The set of variables $\{2, 3, 4\}$ whose values need to be set consistently is not a subset of either 124 or 13. Hence, subproblem $\{234, 45\}$ cannot communicate with $\{124, 13\}$ through a single, representative constraint. Any "agreement" with constraint 124 on the values of x_2, x_4 might conflict with "an agreement" with constraint 13 on the value of x_3 . We would like each subproblem to be "coherent enough" to be able to communicate with other subproblems throughout a single, representative constraint. To formalize this idea, I introduce two definitions due to Gysens et al. (1944).

Definition 5.2: Let $\langle R, E, \ell \rangle$ be the dual graph of some CSP; let $H \subseteq R$, $F \subseteq R - H$ be two sets of constraints. F is connected with respect to H if for any two

constraints c, c' in F , there exists a sequence of constraints $c = c_1, c_2, \dots, c_n = c'$ in F such that for all $i = 1, \dots, n-1$.

- (c_i, c_{i+1}) is an edge in E .
- $l(c_i, c_{i+1})$ contains a variable not in the scope of any of the constraints in H , for each $i = 1, \dots, n-1$.

Intuitively, subproblem F is connected with respect to subproblem H if any two of the constraints in F share, directly or indirectly, variables whose value cannot be set in subproblem H . Hence, even if H is solved and its (partial) solution imposed on F , there may still be extendability and coordination problems in F .

Example 5.1: (continued) Let $H = \{124\}$. Then $F = \{13, 234, 45\}$ is not connected wrt H , because the label 4 on the edge that links 234 to 45 belongs to the scope of a constraint in H . F consists of two connected components wrt H , namely $\{13, 234\}$ and $\{45\}$.

The idea of the “coherent enough” subproblem that can communicate with other subproblems through a single representative is captured in the following definition.

Definition 5.3: Let $\langle R, E, l \rangle$ be the dual graph of some CSP. A hinge is a set of constraints H that contains at least two elements and is either equal to R or a subset of R that satisfies: for each connected component C_i of $R-H$ wrt H , there is a constraint h_i in H such that $\text{scope}(C_i) \cap \text{scope}(H) \subseteq \text{scope}(h_i)$, where the scope of a subproblem is the union of the scopes of its constraints. A hinge is minimal if all its proper subsets are not hinges.

Example 5.1: (continued) The minimal hinges of the CSP defined in Example 5.1 are $H_1 = \{124, 13, 234\}$, $H_2 = \{45, 234\}$, $H_3 = \{45, 124\}$.

Why should CSP's be decomposed into minimal hinges? Two duality-type results provide an answer: decomposition into hinges is the only partitioning method that creates no extendability problems where none exist in the first place.

Definition 5.4: A problem decomposition method preserves extendability if any subproblem F it creates has the following property.

- if every solution of every constraint in R extends to a full solution, then every solution of F extends to a full solution. The next example shows that this is not a trivial property.

Example 5.2: Consider the CSP given by $X=\{x_1, x_2, x_3, x_4\}$, $D_i=\{\alpha, \beta, \gamma\}$, $R=\{12, 23, 34, 14\}$, and $e(12)=\{\gamma\alpha, \gamma\beta\}$, $e(23)=\{\alpha\alpha, \beta\beta\}$, $e(34)=\{\alpha\gamma, \beta\gamma\}$, $e(14)=\{\gamma\gamma\}$. There are two full solutions, $\gamma\alpha\alpha\gamma$ and $\gamma\beta\beta\gamma$. Every solution of every constraint is extendable. The subproblem $\{12, 14, 34\}$, however, has the nonextendable solutions $\gamma\alpha\beta\gamma$, $\gamma\beta\alpha\gamma$; both violate constraint 23.

The next fact, due to Gyssens et al. (1994), shows that the hinge decomposition method preserves extendability. Its proof is in the appendix.

Fact 5.1: Let B be a CSP where every solution of every constraint is extendable. If H is a hinge of B , then every solution of H is extendable.

The next fact shows that the hinge decomposition method is the only one that preserves extendability in all CSP's. Its proof is in the appendix.

Fact 5.2: Let $\langle X, R, s \rangle$ be a CSP skeleton, i.e. a CSP problem whose domains and extents have not been specified. Let F be a subset of R that is not a hinge. Then, there exist domains D_1, \dots, D_n and extents $e(c)$ for each constraint c in R such that in the resulting CSP $\langle X, D, R, s, e \rangle$.

- every solution of every constraint in R is extendable.
- F has a nonextendable solution.

The last fact that makes hinge decomposition interesting is that the size of the largest minimal hinge is an invariant of the dual graph of a CSP; it is due to Gyssens (1986). The size of the largest subproblem of a CSP determines solution time. It makes sense, then, to classify NPD problems into classes representing their degree of difficulty (as measured by the size of their largest minimal hinge); call this parameter the degree of cyclicity of the dual graph of a CSP. The next example shows that there is no relationship between the number of variables of a CSP and its degree of cyclicity, except that the former is an upper bound on the latter. It follows that the number of variables of a problem is not a very precise indicator of its degree of difficulty.

Example 5.3: Consider a sequence A_2, \dots, A_n of CSP's. Each A_k has n variables. The constraint set of each $A_k, k=2, 3, \dots, n$, is $R_k=\{12, 23, \dots, (k-1)k, k1, k(k+1), \dots, (n-1)n\}$. The largest minimal hinge of A_k is the set $\{12, 23, \dots, k1\}$ for $k \geq 2$; its size is k . Hence problems with the same number of variables n can have degrees of cyclicity ranging from 2 to n .

This section has looked at individual subproblems and their properties. The next one discusses how subproblems should be connected with each other. Recall

Clausing's (1994, p.40) statement: "The formation of the best interlocking structure of teams is a key success factor."

6. The best interlocking structure of teams

This section builds on the ideas of sections 4 and 5 to find a way of integrating subproblem solutions that minimizes rework. The basic ideas are three. First, as the results of Section 5 suggest, each subproblem should be a minimal hinge; so that any extendability present in the constraints of the original CSP is preserved. Secondly, as the results of Section 4 suggest, subproblems should be linked to each other to form a binary, tree-structured CSP; so that a solution can be discovered without rework after application of the decision-ordering and communication techniques. Thirdly, given that the size of the largest subproblem determines solution time, subproblems of maximum size should be used as sparingly as possible. I start formalizing these ideas with the notion of a hinge tree, due to Gyssens et al. (1994).

In the next definition, the scope of a hinge is the set of variables that appear in the scope of some constraint in the hinge.

Definition 6.1: Let $G=\langle R,E,I \rangle$ be the dual graph of a CSP. A hinge tree of G is a labelled tree with nodes N , edges A and labelling function λ such that

- (1) Each node in N is a minimal hinge of G .
- (2) Each constraint in R belongs to some node in N .
- (3) If (H,H') is an edge in A , then $H \cap H'$ is a singleton; and $\lambda(H,H')=H \cap H'$.
- (4) If (H,H') is an edge in A , then $\text{scope}(H) \cap \text{scope}(H') = \text{scope}(H \cap H')$.
- (5) If $(H_1,H_2)(H_2,H_3), \dots, (H_{n-1},H_n)$ is a path of edges in A , then $\text{scope}(H_1) \cap \text{scope}(H_n) \subseteq \text{scope}(H_i), i=2,3,\dots,n-1$.

Property 1 was justified in section 5. Property 2 is obviously necessary to cover the original CSP. The next three examples motivate the three remaining properties. (Recall that hinges in the hinge tree correspond to subproblems to be solved independently of each other).

Example 6.1: This example motivates property (3) of a hinge tree. Let B be the CSP defined by $X=\{x_1,x_2,x_3,x_4,x_5\}$ $R=\{12,13,234,235\}$. Its dual graph has R as its

node set; edges (12,13), (12,234), (12,235) (13,234), (13,235), (234,235); and labels of edges, respectively, 1,2,2,3,3,23. This graph contains three minimal hinges, namely $H_1=\{12,13,234\}$ $H_2=\{12,13,235\}$, $H_3=\{234,235\}$. There are two hinge trees satisfying properties (1) (2) and (3), namely these with nodes sets $\{H_i, H_3\}, i=1,2$. There is one hinge tree that satisfies properties (1) (2) but violates property (3), namely $\{H_1, H_2\}$. Problem decomposition $\{H_1, H_2\}$ requires the solution of two subproblems of maximum size; while problem decompositions $\{H_i, H_3\}, i=1,2$, require the solution of only one subproblem of maximum size.

Example 6.2: This example motivates property (4) of hinge trees. Consider the CSP B with $X=\{x_1, x_2, \dots, x_7\}$ and $R=\{23,124,127,135,136\}$. Its dual graph has nodes R ; and there is an edge connecting any two nodes. The minimal hinges are $H_1=\{23,124,135\}$ $H_2=\{23,124,136\}$, $H_3=\{23,127,135\}$, $H_4=\{23,127,136\}$, $H_5=\{124,127\}$ and $H_6=\{135,136\}$. There are two trees that satisfy properties 1, 2 and 3 but violate 4, with node sets $\{H_1, H_4\}$ and $\{H_2, H_3\}$. To see the violation of property 4 by the first of these trees note that $\text{scope}(H_1) \cap \text{scope}(H_4) = \{1,2,3\}$, while $\text{scope}(H_1 \cap H_4) = \text{scope}(23) = \{2,3\}$. The trees that satisfy properties 1 through 4 are those with node sets $\{H_i, H_5, H_6\}$ for $i=1,2,3,4$. Every problem decomposition of the latter form contains only one hinge with three elements; every problem decomposition that violates property 4 contains two hinges with three elements each. Again, a violation of one of the properties of a hinge tree results in larger than necessary subproblem size.

Example 6.3: This example motivates property (5) of hinge trees. Let B be a CSP with $X=\{x_1, \dots, x_7\}$ and $R=\{14,36,47,139,456,123,58\}$. The minimal hinges are $H_1=\{14,36,139,456\}$, $H_2=\{14,36,123,456\}$, $H_3=\{139,123\}$, $H_4=\{47,456\}$, $H_5=\{58,456\}$. The trees of hinges that satisfy properties 1 through 4 but violate property 5 have node sets $\{H_i, H_m, H_j, H_n\}$ where $i \neq j, i, j=1,2$ and $m \neq n, m, n=4,5$; and edges (H_i, H_m) , (H_m, H_j) , (H_j, H_n) , all labelled with 456. The trees of hinges that satisfy all five properties have node sets $\{H_i, H_3, H_4, H_5\} i=1,2$; and edges (H_i, H_3) , (H_i, H_4) (H_i, H_5) ; the first edge labelled with 123 and the other two with 456. Again, the trees of hinges that satisfy all five properties involved only one hinge of maximum size; while all those trees of hinges that satisfy only the first four properties involve two hinges of maximum size, resulting in larger than necessary subproblem size.

I now describe how exactly a hinge tree is used to solve a CSP. There are three ideas involved: problem decomposition into minimal hinges; subproblem communication through the edges of the hinge tree; and solving not the original CSP (by picking values for each individual variable out of its domain), but an equivalent, dual CSP (by picking tuples of values out of each subproblem's solution set). The basic construction is described by the next definition.

Definition 6.2: Let $B = \langle X, D, R, s, e \rangle$ be a CSP, $G = \langle R, E, I \rangle$ its dual graph, and $\langle N, A, \lambda \rangle$ a hinge tree of G . The dual CSP of B is defined to be a binary tree-structured CSP $B' = \langle X', D', R', s', e' \rangle$, as follows.

- $X' = N; R' = A; s'(H_1, H_2) = \{H_1, H_2\}$ for each (H_1, H_2) in R' .
- for each hinge H in N , $D'_H =$ solution set of H
- for each edge (H_1, H_2) in A , $e'(H_1, H_2) =$ all pairs (u^1, u^2) where u^i is a solution of $H_i, i=1,2$; and where u^1 and u^2 assign the same values to the variables they share, i.e. to the variables in $\text{scope}(H_1) \cap \text{scope}(H_2)$.

The dual of a CSP, being binary and tree structured, can be solved without rework, after the methods of Section 4 have been applied. The next example takes us through the steps of the solution process, assuming that a hinge tree has already been constructed and the solution sets of the hinges computed.

Example 6.4 The CSP B is defined by $X = \{x_1, x_2, \dots, x_9\}; D_i = \{\alpha, \beta, \gamma, \delta\}, i = 1, 2, \dots, 9; R = \{12, 1345, 238, 456, 57, 67, 89\}; e(12) = \{\alpha\alpha, \beta\beta, \gamma\gamma, \delta\delta, \alpha\beta, \beta\alpha\}, e(1345) = \{\alpha\beta\beta\alpha, \beta\gamma\gamma\beta, \gamma\delta\delta\gamma, \delta\delta\delta\delta\}, e(238) = \{\alpha\gamma\delta, \alpha\beta\alpha, \beta\gamma\beta, \gamma\delta\gamma, \delta\delta\delta\}, e(456) = \{\gamma\gamma\alpha, \beta\alpha\alpha, \delta\gamma\beta, \delta\delta\delta\}, e(57) = \{\alpha\alpha, \beta\beta, \gamma\gamma, \delta\delta\}, e(67) = \{\alpha\alpha, \beta\beta, \gamma\gamma\}, e(89) = \{\alpha\alpha, \delta\delta\}.$

A hinge tree of B has nodes H_1, H_2, H_3, H_4 where $H_1 = \{12, 1345, 238\}, H_2 = \{1345, 456\}, H_3 = \{456, 57, 67\}, H_4 = \{238, 89\};$ and edges $(H_1, H_2), (H_2, H_3), (H_1, H_4)$, labelled, respectively, with 1345, 456, 238. The solution sets of each hinge are given by

$$D_{H_1} = \{x_1 x_2 x_3 x_4 x_5 x_8 = \beta\beta\gamma\gamma\beta\alpha, \gamma\delta\delta\gamma\gamma, \delta\delta\delta\delta\delta\delta, \alpha\alpha\beta\beta\alpha\alpha, \beta\alpha\gamma\gamma\beta\alpha\},$$

$$D_{H_2} = \{x_1 x_3 x_4 x_5 x_6 = \gamma\delta\delta\gamma\beta, \delta\delta\delta\delta\delta, \alpha\beta\beta\alpha\alpha\},$$

$$D_{H_3} = \{x_4 x_5 x_6 x_7 = \gamma\gamma\alpha\alpha, \beta\alpha\alpha\alpha, \delta\delta\delta\delta\},$$

$$D_{H_4} = \{x_2 x_3 x_8 x_9 = \alpha\gamma\delta\delta, \delta\delta\delta\delta, \alpha\beta\alpha\alpha\}.$$

A width-one ordering of the hinge-tree is $H_1 < H_2 < H_3 < H_4$. The parent of H_4 and H_2 is H_1 , and the parent of H_3 is H_2 . The DAC algorithm starts from H_4 , and eliminates from D_{H_1} all tuples inconsistent with all values in D_{H_4} ; since H_1 and H_4 share the variables 238, every solution of H_1 that does not agree with any solution of H_4 on the variables 238 is eliminated. We get $D'_{H_1} = \{x_1 x_2 x_3 x_4 x_5 x_8 = \delta\delta\delta\delta\delta\delta, \alpha\alpha\beta\beta\alpha\alpha, \beta\alpha\gamma\gamma\beta\alpha\}$ i.e. the first two solutions of H_1 are eliminated by the DAC algorithm.

The DAC algorithm now proceeds to the hinge immediately preceding H_4 in the width-one ordering, namely H_3 ; and eliminates from D'_{H_2} (the domain of the parent of H_3) all tuples that do not agree on the variables 456 with any tuple in D'_{H_3} . The resulting domain of H_2 is $D'_{H_2} = \{x_1x_3x_4x_5x_6 = \delta\delta\delta\delta\delta, \alpha\beta\beta\alpha\alpha\}$, i.e. H_2 has lost one solution. Finally, the DAC algorithm proceeds to H_2 , and eliminates from D'_{H_1} (the domain of the parent of H_2) all tuples that do not agree on the variables 1345 with any tuple in D'_{H_2} . The resulting domain of H_1 is $D''_{H_1} = \{x_1x_2x_3x_4x_5x_8 = \delta\delta\delta\delta\delta\delta, \alpha\alpha\beta\beta\alpha\alpha\}$, i.e. H_1 has lost one more solution. The BT algorithm now takes over from the DAC algorithm.

It starts from the first value of the first variable in the dual CSP, i.e. from the tuple $x_1x_2x_3x_4x_5x_8 = \delta\delta\delta\delta\delta\delta$ in D''_{H_1} . It proceeds to the next dual variable, i.e. H_2 , and discovers that $x_1x_3x_4x_5x_6 = \delta\delta\delta\delta\delta$ is consistent with its previous assignment. It then proceeds to H_3 , H_4 , in that order, and discovers that an assignment of δ to all variables in the scope of each hinge is consistent with all previous assignments. The BT algorithm terminates with the solution $x_i = \delta$, all i , without having performed any rework, since no assignment of δ 's to each hinge's scope ever had to be undone. If the BT algorithm had started from the other value in D''_{H_1} , namely $\alpha\alpha\beta\beta\alpha\alpha$, it would have extended it without rework to the other full solution, namely $\alpha\alpha\beta\beta\alpha\alpha\alpha$.

7. Costs and benefits of organizing for fast NPD

The previous sections have shown that a decision-ordering, a communication, and a problem-partitioning technique will solve a CSP without any rework between subproblems. What is the overall cost of applying these methods, and how does it compare with the cost of solving a CSP without them? Given that typical NPD problems are large (recall the figures cited in point six of the introduction), it makes sense to adopt rate of growth as our measure of cost. To see what this means, recall that in section 4 it was seen that to solve binary, tree-structured problems we need to perform n constraint checks to obtain a width-one ordering; nk^2 constraint checks to obtain arc consistency, and nk constraint checks to solve the resulting CSP. The overall cost is thus $n + nk + nk^2$. Considering only the rate of growth means replacing this expression by its leading term, ignoring its coefficient. Hence

Fact 7.1 The cost of solving a binary, tree-structured CSP is k^2 , where k is the size of its largest domain.

This is standard computer science practice. Cormen et al. (1990, p. 10), state: "It is the rate of growth of the running time that really interests us. We therefore consider only the leading term of a formula since the lower order terms are relatively insignificant for large n . We also ignore the leading term's constant coefficient, since constant factors are less significant than the rate of growth in determining computational efficiency for large inputs".

Recall also that to solve an arbitrary CSP we need rk^n constraint checks. Hence

Fact 7.2 The cost of finding a solution of an arbitrary CSP with the (unaided) BT algorithm is k^n .

To apply the methods of section 6, we need to compute the solution sets of subproblems of the original CSP, as opposed to finding a single solution. How is this done? If B is the CSP whose solution set we seek, apply the BT algorithm to its dual CSP, with one difference; once the first solution is identified, instead of stopping, discard the portion of the search tree already explored by the BT algorithm, and apply the BT algorithm to the rest. Stop when the whole search tree has been explored; any time a new solution is identified, add it to the solution set. If the size of the extends of the constraints in the original CSP has maximum ℓ , and if there are r constraints in the original CSP, the solution set can be computed after at most l^r constraint checks. Hence, if d is the degree of cyclicity of the dual graph of a CSP, computing the solution set of any subproblem that is a node of a hinge tree takes at most l^d constraint checks, since d is the maximum number of constraints any such subproblem may contain.

Fact 7.3 The cost of computing the solution sets of the subproblems that are the nodes of a hinge tree is l^d .

To apply the methods of section 6 we need an algorithm that computes a hinge tree. Here is what the algorithm basically does. It picks some constraint c in R and computes the connected components C_1, \dots, C_m of $R - \{c\}$ wrt c . It then forms the hinges $H_i = C_i \cup \{c\}$; and the tree with nodes H_1, \dots, H_m , edges (H_i, H_{i+1}) $i = 1, \dots, m - 1$, and labels of all edges c . It then marks c as used, and repeats the same process with some H_i that contains more than two elements, and at least one unused element. It stops when all constraints have been marked used, or when all nodes in the constructed tree contain only used elements. In case $R - \{c\}$, or some $H_i - \{c\}$, contains only one connected component wrt c , c is marked used, another, unused constraint is picked, and the process repeated. The cost of this algorithm is actually the cost of computing connected components;

connected components are computed by standard graph algorithms (Cormen et al. (1990, p. 488)).

Fact 7.4 (Gyssens et al. (1994)). The cost of computing a hinge tree is r^2 , where r is the number of constraints of the original CSP.

Note also that the number of nodes in a hinge tree is bounded by r , since hinges are constructed as connected components of subsets of R until R is covered.

Finally, the methods of section 6 require the discovery of a solution of a binary, tree structured CSP using the methods of section 4. The variables of this CSP are the nodes of the hinge tree. We know from fact 7.1 that the cost of solving such a problem is determined by the size of the largest domain of the CSP, i.e., in our case, by the size of the largest solution set pertaining to a node of the hinge tree. This is no larger than ℓ^d , where ℓ is the size of the largest extent of a constraint and d the number of constraints in the largest minimal hinge. Hence by fact 7.1

Fact 7.5 The cost of finding a solution to the dual CSP defined by the hinge tree of the original CSP is ℓ^{2d} .

By facts 7.3, 7.4 and 7.5 we have that the sum of costs of applying the methods of section 6 is $r^2 + \ell^d + \ell^{2d}$. Hence, neglecting all but the leading terms, we obtain

Fact 7.6 The cost of finding a solution to a CSP using the decision-ordering, communication and problem-partitioning techniques is ℓ^{2d} .

Comparing ℓ^{2d} with k^n , we conclude that the organizational methods that eliminate rework between subproblems are worth their cost if the degree of cyclicity d of a CSP is small relative to the number of variables n of the same CSP.

8. Conclusion

This paper considers technological change, and in particular new product and process development, from a new perspective, that of complex problem-solving. Technological change is made possible by organizational techniques that reduce the complexity of problem-solving; differences in the technological performance of firms are attributed to their different problem-solving styles. More specifically, this paper proposes the formalism of constraint satisfaction

problems (CSP) as (a) expressive enough to capture design problems, including design for manufacturing, listening to the voice of the customer, and robust design; and (b) tractable enough to be fully decidable, i.e. to possess an algorithm that will always correctly generate a solution, or the set of all solutions. This algorithm produces too much rework; in fact, rework is the main reason and symptom of slow new product development, both on theoretical and empirical grounds. To minimize rework, this paper proposes three distinct techniques. A technique to order decisions; a technique to make more specific the goals of design by communication prior to decision-making; and a problem-partitioning technique that minimizes subproblem size subject to the constraint of not creating extra extendability or coordination problems. The three techniques together provably minimize rework and thus accelerate decision-making. The problem-partitioning technique in particular associates with each design problem a tree of subproblems; the size of the largest subproblem is an index of the degree of difficulty of the design problem. The nature of the technical and marketing constraints faced by product designers determines both the organizational form (the tree of subproblems) appropriate for the design problem and the speed of reaching a solution (an exponential term whose exponent is the size of the largest subproblem). This organizational form is reusable because it depends only on structural information, i.e. on which variables enter which constraints, not on the values that satisfy each constraint. The cost of building this organizational form is quadratic in the size of the design problem, i.e. other things being equal, larger firms with many interdependent products face disproportionately larger costs of adjusting their organizational forms to changes in the underlying structural information. If the underlying structure remains the same, though, an incumbent firm that has already computed its organizational form can amortize it over many different NPD efforts, and will develop new products faster than a new entrant who still has to figure out how to organize for new product development.

The empirical literature on new product development stresses the importance of design in determining operational efficiency. Baily and Gersbach (1995, p. 347) summarizing their findings on the determinants of operating efficiency, state "Traditional determinants, such as capital intensity and scale were found to play a role. But innovations such as design for manufacturing and workplace organization turned out to be even more important". The empirical literature by itself, however, cannot pinpoint exactly how fast product developers differ from slow product developers; a result of this is that it is not clear to slow developers what they should be imitating to become fast product developers. Ward et al. (1995) make this point clearly in their discussion of Toyota's NPD organization, which they call set-based concurrent engineering: "We do not know enough about how set-based concurrent engineering is or should be performed. Toyota's approach is not well-defined or documented", and "Since there is no proven formal methodology, learning the process will be slow and error-prone".

Furthermore, the empirical literature has not established causal relationships between time and problem-solving techniques; only associations have been documented. Ward et al. (1995) state "Each advantage of set-based concurrent engineering described earlier represents a hypothesis - that there is a causal relationship between Toyota's success and its use of set-based concurrent engineering. An important task for further research is therefore to demonstrate this causal link more carefully. Unfortunately such causes are difficult to show in complex organizations". Seen in this light, this paper contributes a well-defined set of techniques that provably accelerate NPD; these techniques could, therefore, provide a starting point for filling this gap in the literature.

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