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Telecommunications:
A Robustness Analysis

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# Efficiency Measurement and Regulation in U.S. Telecommunications: a Robustness Analysis* 

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#### Abstract

The paper investigates the robustness of different efficiency measures that can support the implementation of diverse forms of incentive regulation in the context of U.S. telecommunications. Comparisons, in terms of an output orientation, are considered for efficiency scores obtained from Data Envelopment Analysis (DEA), distance function (with corrected ordinary least squares and a random effects model) and distance function embedded in a stochastic frontier framework (with time invariant, time varying efficiencies or with inefficiency effects). Similarly to the previous empirical literature, one finds, in most cases, only a moderate consistency across the different approaches. In fact, the different spectrum of techniques imposed varied degrees of structure in the error term and indicated non-negligible discrepancies across the different measurement approaches in terms of the ranking structure, degree of persistence and best and worst practices patterns.


Key-words: efficiency measurement, yardstick regulation
JEL classification: D29, L59, L96

[^0]
## Introduction

The relevance of asymmetric information in regulated settings is by now largely recognized [see Laffont and Tirole (1993) for a comprehensive overview of the theoretical literature]. Yardstick regulatory schemes have been suggested as a possible relevant mechanism for partially mitigating the aforementioned asymmetries. Assuming that comparable and spatially separated utilities prevail, those approaches could, even if not directly implemented, provide useful guidance for designing incentive regulation schemes and setting the productivity offset. The relevance of different efficiency measurement techniques for devising benchmarking schemes was highlighted, for example, by Granderson and Linvil (1999) for natural gas transmission in the U.S. and by Tupper and Resende (2004) in the context of water and sewerage services in Brazil.

An essential step towards the implementation of any yardstick scheme pertains the adequate measurement of efficiency. In the context of telecommunications different contributions emerged in terms of nonparametric frontiers as exemplified by Majumdar (1995, 1997), Resende (2000), Uri (2001), Façanha and Resende (2000) and Resende and Façanha (2005) and distance functions as given by Uri (2002, 2003). An important focus of some of the previous studies referred to the efficiency and servicequality features of different regulatory regimes.

It is important, however, to further investigate the robustness of the efficiency scores under different approaches. With that respect, the literature
is yet limited, and it is worth mentioning the works by Bauer et al (1998), Coelli and Perelman (1999) and Berg and Lin (2006) as respectively applied to financial institutions, railways and water utilities. The evidence indicates some robustness for a subset of techniques. In the present paper, one intends to undertake a broader spectrum of efficiency measurement techniques in the context of U.S. telecommunications. For that purpose, models with an increasing complexity in terms of the specification of the stochastic component are compared. Specifically, Data Envelopment Analysis-DEA nonparametric efficiency frontiers, traditional distance function and yet variants of models with distance functions embedded within a stochastic frontier framework.

The paper is organized as follows. The second section summarizes the conceptual aspects related to efficiency measurement in the context of the selected approaches. The third section discusses the data construction procedures and presents and compares the results accruing from the different approaches. The fourth section brings some final comments and suggestions for future research.

## 2. Efficiency Measurement: Some Conceptual Aspects

## 2.1-Introduction

A central feature of the telecommunications sector pertains its multi-output feature. Therefore, it is important to consider technology descriptions and measurement methods that properly deal with that aspect but are yet flexible
in terms of data requirement. In fact, the most traditional cost function estimation or even stochastic cost frontiers require input prices data. In the context of U.S. telecommunications, one can highlight the applications considered by Shin and Ying (1992), Ying and Shin (1993) and Resende (1999) that considered flexible Translog cost function estimation with similar data construction procedures. It is possible, however, to ponder that deflating and user cost procedures make input prices construction difficult and potentially subject to criticisms [see e.g. by Gasmi et al. (2002)]. In this sense, from a practical perspective, it is relevant to consider multi-output approaches that require only quantity data but not necessarily in terms on nonparametric procedures.

The robustness exercise carried out in the present paper follows that route by considering the unifying notion of distance function. The concept outlined by Shephard (1970) is overviewed in Kumbhakar and Lovell-KL (2003). A distance function completely describes the technology and can be defined in terms of radial contraction or expansion movements depending on whether one focuses on input conservation or output expansion.

A basic working definition relates to the notion of output set considered in a setting with K inputs and M outputs and describes the set of output vectors that are feasible for each input vector $\mathrm{x} \in R_{+}^{K}$, more precisely:

$$
\begin{equation*}
P(x)=\left\{y \in R_{+}^{M}: x \text { can produce } y\right\} \tag{1}
\end{equation*}
$$

The output distance function provides the minimum amount by which an output can be deflated and still remain feasible with a given input vector. In
other words, one is considering feasible radial output expansion movements.
Specifically:

$$
\begin{equation*}
D_{o}(x, y)=\min \{\theta:(y / \theta \in P(x)\} \tag{2}
\end{equation*}
$$

The properties of the output distance function follow from the properties of the output set and amongst those it is worth mentioning that $\mathrm{D}_{\mathrm{o}}(\mathrm{y}, \mathrm{x})$ is nondecreasing, convex in y a homogeneous of degree 1 in output [see KL for details]. In particular, the last property implies that $D_{O}(x, \omega y)=\omega D_{O}(x, y)$ for any $\omega>0$ and in empirical practice will be contemplated upon output normalizations. ${ }^{1}$ Next, different approaches based on that concept are briefly outlined.

## 2,2- Nonparametric approximation of the distance function

An influential and by now largely established approach is provided by Data Envelopment Analysis-DEA. This mathematical programming approach is extremely flexible and has given rise to a broad range of applications in different contexts. [see Cooper et al (2000) for an overview]. Unlike traditional econometric approaches that highlight average behaviours, that technique focuses on local comparisons to generate relative efficiency scores. A traditional formulation under variable returns to scale was advanced by Banker, Charnes and Cooper (1984)-BCC. Under an output orientation, one can conceive a situation where the aim is to maximize the ratio of a virtual

[^1]output (composed as a weighted average of outputs) relative to a virtual input (composed as a weighted average of inputs) subject to non-negativity constraints on weights, a restriction imposing an upper bound for the efficiency scores and yet a convexity restriction given the variable returns to scale assumption. In the output oriented BCC model an equivalent linear programming program is solved for each for each decision making unit (DMU) $(\mathrm{j}=1, \ldots, \mathrm{~J})$ and here specified for the i -th unit. as follows:. The solution will enable to generate relative efficiency scores:
\[

$$
\begin{equation*}
\max _{\phi_{i}, \lambda_{i}, s_{i}^{-}, s_{i}^{+}} T_{i}=\phi_{j}+\varepsilon \sum_{k=1}^{K} s_{i k}^{-}+\varepsilon \sum_{m=1}^{M} s_{r k}^{+} \tag{3}
\end{equation*}
$$

\]

Subject to:

$$
\begin{gather*}
\sum_{j=1}^{J} \lambda_{j i} x_{k j}+s_{k i}^{-}=x_{k i} \quad k=1, \ldots, K \\
\sum_{j=1}^{J} \lambda_{j i} y_{m j}-s_{m i}^{+}=\phi_{i} y_{m i} \quad m=1, \ldots, M \\
\sum_{j=1}^{J} \lambda_{j i}=1  \tag{6}\\
\lambda_{j i} \geq 0  \tag{7}\\
s_{k i}^{-} \geq 0  \tag{8}\\
s_{m i}^{+} \geq 0 \tag{9}
\end{gather*}
$$

Where $\varepsilon$ denotes a non-Archimedian quantity ( $0<\varepsilon<1 / \mathrm{N}$ for any positive integer N ) and $s_{m i}^{+}$and $s_{k i}^{-}$indicate slacks. A DMU i is considered to be efficient if $\phi_{i}=1$ and zero slacks prevail. In the application, given the panel data structure of the data. It is considered a window analysis procedure
where each DMU is compared with the other DMUs and with itself in different periods. The largest possible window with 13 periods is considered.

## 2.3- Parametric approximation of the distance function

### 2.3.1- Traditional econometric estimation

Despite the flexibility of the notion of distance function, empirical applications, as previously mentioned, have been scarce. A first step refers to a flexible parameterization where the Translog function can play a relevant role. The steps for the empirical implementation are detailed, for example, in Lovell et al (1994) and Coelli and Perelman (2000). Under the referred parameterization one has:

$$
\begin{align*}
& T L \equiv \ln D_{O i}=\alpha_{0}+\sum_{m=1}^{M} \alpha_{m} \ln y_{m i}+\frac{1}{2} \sum_{m=1}^{M} \sum_{n=1}^{M} \alpha_{m n} \ln y_{m i} \ln y_{n i}+\sum_{k=1}^{K} \beta_{k} \ln x_{k i} \\
& +\frac{1}{2} \sum_{k=1}^{K} \sum_{l=1}^{K} \beta_{k l} \ln x_{k i} \ln x_{l i}+\sum_{k=1}^{K} \sum_{m=1}^{M} \delta_{k m} \ln x_{k i} \ln y_{m i} \tag{10}
\end{align*}
$$

The homogeneity of degree 1 in outputs can be expressed in terms of the following conditions:

$$
\begin{equation*}
\sum_{m=1}^{M} \alpha_{m}=1 ; \quad \sum_{n=1}^{M} \alpha_{m n}=0 \quad m=1,2, . ., M ; \quad \sum_{m=1}^{M} \delta_{k m}=0 \quad k=1,2, . ., K \tag{11}
\end{equation*}
$$

The symmetry conditions, on the other hand, require:

$$
\begin{equation*}
\alpha_{m n}=\alpha_{n m} \quad m, n=1,2, . ., M \quad \beta_{k l}=\beta_{l k} \quad k, l=1,2, \ldots, K \tag{12}
\end{equation*}
$$

One is seeking a context where $-\infty<\mathrm{D}_{\mathrm{oi}}<1$ where $\mathrm{D}_{\mathrm{Oi}}=1$ indicates a point in the efficiency frontier. .The homogeneity condition, as implied by section 2.1, can be easily imposed by normalizing expression (10) by an arbitrary output (say $\mathrm{y}_{\text {мі }}$. Thus proceeding, one readily obtains:

$$
\begin{equation*}
-\ln \left(y_{M i}\right)=T L(.)-\ln \left(D_{O i}\right) \quad i=1,2, \ldots, N \tag{13}
\end{equation*}
$$

The key step in the empirical implementation is to reinterpret the $-\ln \left(\mathrm{D}_{\mathrm{oi}}\right)$ as an usual error term for econometric estimation. Assuming a simple bilateral structure for the error term, one can make use of a corrected ordinary least squares (COLS) procedure to obtain positive efficiency scores. Specifically, one considers in the case of the output orientation, $\exp (($ maximum negative residual)-(residual)) In other words, one adjusts the residuals in the opposite direction of a shift in the intercept so as to obtain meaningful positive efficiency scores. The OLS procedure, of course, imposes a strong stochastic assumption. A more flexible possibility for the estimation of distance functions, but usually ignored, would be to consider an analogous residual correction but with a random effects panel data model. In that case, a sub-component of the error term would be firm-specific and the resulting estimates would be more likely to capture unobserved heterogeneities. The two procedures in the empirical application will be denoted respectively by DF-OLS and DF-RE.
2.3.2- Distance function embedded in a stochastic frontier analysis framework A usual criticism to non-parametric efficiency measurement approaches like DEA refers to its nearly deterministic character. In fact, discrepancies across different $f$ units are solely attributed to inefficiencies. SFA, on the other hand, considers a composed error terms that separates efficiency and statistical noise but at the price of specific functional forms assumptions. ${ }^{2}$ Nesting flexible multi-output distance function approaches within a SFA framework is

[^2]relatively uncommon and an exception is provided by Morrison Paul et al (2000). Standard procedures for SFA estimation readily follow when one considers a distance function approach except for a change in the sign of the error terms. In fact, in the efficiency frontier $\ln \left(\mathrm{D}_{\mathrm{oi}}\right)=0$ imply that the composed error term will be reversed as $\left(u_{i}-v_{i}\right)$ where the sub-components respectively stand for the statistical noise and technical efficiency. In order to conform with the standard SFA framework, one can change the sign of the dependent variable in standard software implementation and take care with the reversed interpretation of the coefficients. ${ }^{3}$

Among the large literature on SFA methods for panel data, it is worth emphasizing two works. Battese and Coelli (1992) considered a model with time-varying efficiency such that:

$$
\begin{equation*}
u_{i t}=\eta_{i t} u_{i}=\{\exp [-\eta(t-T)]\} u_{i} \quad i=1, \ldots, N \tag{15}
\end{equation*}
$$

In this model $U_{i t}$ decreases, remains constant or increases with time if $\eta>0$, $\eta=0$ or $\eta<0$ respectively. In the application, it always be considered the simplified setup of the normal/truncated-normal model where $\mathrm{v}_{\mathrm{it}}$ and $\mathrm{u}_{\mathrm{it}}$ are respectively assumed to be independent and identically distributed as $\mathrm{N}\left(0, \varpi_{V}^{2}\right)$ and $\mathrm{N}^{*}\left(\mu, \sigma_{u}^{2}\right)$, where former stands for a non-negative truncated normal distribution; Moreover, one assumes independence between those error subcomponents We will consider in the application a model with time-varying efficiency (DF-SF-TN2) and the special case where $\eta=0$ and the efficiency scores only display cross-sectional variation (DF-SF-TN1).

[^3]Finally, it is important to highlight a class of models with inefficiency effects as advanced by Battese and Coelli (1995). In this model, one incorporates the possibility that the mean of the efficiency error sub-component can be explained by other variables. More precisely, $\mu_{i t}=z_{i t} \delta$, where $\mathrm{z}_{\mathrm{it}}$ denotes a (1 x r) vector of explanatory variables whereas $\delta$ indicates the associated ( $r \times 1$ ) vector of unknown parameters. This model will be referred as DF-SF-TN3.

## 3. Empirical Analysis

## 3.1-Data construction

The main data source of the present is the Statistics of Communication Common Carriers made available by the Federal Communications Commission. Given consolidations and some omissions, special care was taken to construct a balanced consistent panel of firms. The final sample comprises 30 local telephone companies (LECs) over the 1988-2000 period. The list of LECs in the sample is presented in appendix 1.

In order to explore the flexibility of the distance function approach, physical measures for inputs and outputs were considered whenever it was possible. The following inputs and outputs were considered:

Inputs
EMP: total number of employees;
..COS: total number of central office switches;
. CAB: total miles of cable;
. MAT: quantity of materials approximated by (Operating Expenses- Labor Expenses-Depreciation Expenses) deflated by the general implicit price deflator for telecommunications $(1996=100)$ obtained from the U.S. Bureau of Economic Analysis;

## Outputs

. LOC: number of minutes-local calls;
. TOLL: number of minutes-toll calls ;
ACC: number of minutes-access

Moreover. it is worth mentioning that ACC was used as the normalizing output to impose the homogeneity restriction and that in the model with inefficiency effect (DF-SF-TN3), a time trend was considered as the only explanatory factor affecting the mean of the (efficiency) error sub-component.

## 3.2- Comparing efficiency assessments: conceptual aspects

Even though efficiency measurement constitute an important element towards efficiency-based regulation, one encounters yet relatively few robustness exercises. In that sense, it is worth mentioning the evidence obtained from some selected studies for utilities. Coelli and Perelman (1999) considered European railways and undertook a comparative assessment of efficiency measures obtained from DEA, parametric linear programming (PLP) and distance function with COLS, under both input and output orientation. The evidence indicates strong correlation patterns across different techniques,
especially in what concerns PLP and COLS. Berg and Lim (2006) considered the Peruvian water sector and compared the efficiency scores obtained from DEA (under different specifications) and an input distance function nested within a stochastic frontier framework-DF-SFA. In their case, the major focus of comparison related to an actual yardstick scheme implemented in that country (the SUNASS evaluation). In general terms, it is detected a moderate consistency in terms of rank correlations between DEA and the DF-SFA scores. Moreover, as is often the case, there is a high coherency between the DEA scores obtained from different orientations. The work by Bauer et al (1998) considered financial and undertook a comparative assessment of efficiency measurement with DEA, SFA, thick frontier approach (TFA) and distribution-free approach (DFA) and is particularly worth mentioning for suggesting guidelines for comparing the results from different measurement techniques. Before proceeding with the consistency analysis of the paper, let's briefly consider some features of the efficiency scores presented in tables A1 through A6 in the appendix. In contrast with previous comparative exercises, one assesses the robustness of different approaches taking as reference the unifying notion of a distance function for comparing DEA, DFOLS, DF-RE, DF-SF-TN1, DF-SF-TN2 and DF-SF-TN3. As mentioned before, the models vary in complexity by either specifying no structure for the stochastic term, specifying a bilateral error or yet a composed error structure. The former case occurs with the nesting of a distance function within a SFA framework that can incorporate or not time-varying efficiencies and
inefficiency effects. The possible combinations are numerous and the six models exhibit important discrepancies and patterns in a first inspection of the tables A1 through A6 displayed in appendix 2, most notably: ${ }^{4}$
i) The evolution of efficiency is not always monotonic and erratic trajectories occasionally prevail with abrupt reversals as for example in the case of DF-OLS;
ii) Substantial underperformance arises in the case of the SFA methodologies
iii) Model explicitly allowing for time-varying efficiencies like DF-SF-TN2 indicate negligible changes in efficiency.

Some relevant consistency criteria would be as follows;
a) Comparisons of efficiency distributions with each other

The authors compared descriptive statistics in general for the different efficiency scores and paid particular attention to the temporal evolution of the average efficiency under the different approaches. As expected, one detected great discrepancies across the absolute values of those average scores. In fact, one should remember in particular that DEA scores are obtained from local efficiency comparisons whereas econometric-based models always impose some kind of average behavior. A more fruitful approach would be the focus on co-movements rather than the absolute values of the scores. In that sense, a multivariate analysis of the stacked efficiency scores vectors can be

[^4]useful. In order to detect the presence of common dimensions among the different measures of efficiency, the multivariate statistical technique of principal components analysis-PCA can be appropriate. The technique considers linear combinations of the $p$ original variables $X_{j}^{\prime} s(j=1, \ldots, p)$ with generic expression for the i-th principal component given (with a slight abuse of notation) by:
$$
Z=a_{i 1} X_{1}+\ldots .+a_{i p} X_{p}
$$

The coefficients of the linear combination are established such that the first principal component captures the most expressive part of data variation. The following principal components capture a decreasing portion of the data variation. The principal components are pairwise orthogonal in the sense that different principal components capture independent dimensions of the data. ${ }^{5}$ A common criterion for assessing the contribution of the different principal components relates to the magnitude of the eigenvalues of the correlation matrix of the original data ${ }^{6}$ and one would retain those that exceed 1 or yet seek a cumulative variance of more than some specified value (typically 75\%) The evidence accruing from the PCA is summarized in tables 1 and 2, and indicates that under both criteria one should retain only the first 2 principal components and therefore it is possible to detect important common dimensions and co-movements across the efficiency scores obtained from the alternative techniques. Moreover, the positive coefficients of the components matrix with respect to the first component reflects a general efficiency

[^5]component whereas one observes negative coefficients of the second component with respect to DF-RE, DF-SF-TN1and DF-SF-TN2. Even though, the results are not clear cut they might indicate that the allowance for persistence in the error term differentiate some efficiency measures beyond the capacity of capturing a common overall efficiency.

## INSERT TABLES 1 AND 2 AROUND HERE

b) Rank order correlation of the efficiency distributions

The consideration of yardstick schemes poses an important role to the order structure of efficiency scores. In fact, one should seek a reasonable coherency in terms of rank correlations between different measures. Otherwise, specific measures must be carefully chosen with some a priori justification. The evidence is presented in table 3 below.

## INSERT TABLE 3 AROUND HERE

In general only moderate coherency arises between the different measures though some relatively high correlations are present between some distance function approaches (direct econometric estimation and some versions embedded with SFA). The observed magnitudes are not strikingly contrasting with previous evidence obtained by Bauer et al (1998) and Berg and Lim (2006) in different sectors and in part with different measurement approaches.

The results therefore suggests that there are important differences in the order structure across distinct efficiency measures.

## c)Identification of Best-Practice and Worst-Practice Firms

Even though the coherence in terms of rank correlations might be limited in occasions one might be interested in inspecting more closely the tails of distributions of efficiency scores. Indeed, from a benchmarking perspective, a good capacity of identifying best-practice and worst-practice units could still be useful. The related evidence is presented in table 4.

## INSERT TABLE 4 AROUND HERE

The evidence indicates the proportion of matching between pairs of techniques for the top $20 \%$ and lower $20 \%$ utilities. The matching coherency is only moderate and with similar magnitudes as those obtained by Bauer at al (1998) in a different context. Moreover, one does not notice any particularly asymmetric ability on detecting best or worst practices.

## d) Stability of Measured Efficiency over Time

From a regulatory perspective, one should seek efficiency patterns that display some relative stability or consider some average behavior within some carefully chosen time window. Next, table 5 indicates the persistence of efficiency by considering the average correlations for different time intervals. The evidence is not always clear cut as in some cases a substantial proportion of non-significant correlations arise. The trivial case of the DF-SFTN1 model is not reported as it imposes time-invariant efficiencies. For the
other approaches one detects a substantial degree of persistence with very slow decay as the time distance increases with the exception of DF-OLS that initially displays moderate values for the correlations that rapidly decline afterwards. the movements just described were predominantly monotonic. In summary, persistence appears to be an important feature and might be potentially interested in adopting techniques that explicitly account for that stylized fact.

## INSERT TABLE 5 AROUND HERE

## 4. Final Comments

The paper aimed at investigating the robustness of different efficiency measurement approaches in the context of the U.S. telecommunications as potentially supportive to incentive regulatory practices. The paper adopted the unifying concept of a distance function to characterize a multi-output technology in a flexible manner. Similarly to the previous empirical literature, one finds, in most cases, only a moderate consistency across the different approaches. In fact, the different spectrum of techniques imposed varied degrees of structure in the error term and indicated non-negligible discrepancies across the different measurement approaches in terms of the ranking structure, degree of persistence and best and worst practices patterns.

Even though, the stochastic frontier literature provides a more precise modeling of the error sub-components in terms of statistical noise and efficiency it possesses shortcomings related with the specific functional form
assumptions. Moreover, a reliable estimation require relatively large panel data sets that would extrapolate a typical regulatory period of 4-5 years, whereas a long panel only would be meaningful in the case of less dynamic industries. This last aspect underscores the fact that yardstick schemes are more feasible in sectors with a simple technology like the water industry for example. In fact, rapid technical changes observed in the telecommunications industry make the utilization of long panels questionable. ${ }^{7}$

The aforementioned caveats indicate a possible useful role for nonparametric efficiency measurement methods like DEA that displayed some consistency with the more general specification of the SFA approach with inefficiency effects (in this paper DF-SF-HN3); The flexibility of nonparametric approaches can be relevant in regulatory settings, but in that case a careful stochastic treatment by means of bootstrap re-sampling methods can be valuable [see e.g. Simar (1992)].

[^6]
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## Table 1

Principal Components for Efficiency Scores across Different TechniquesExplained Variance

| Principal components | variance | proportion of <br> total variance (\%) | cumulative <br> proportion of <br> total variance (\%) |
| :---: | :---: | :---: | :---: |
| 1 | 3.624 | 60.408 | 60.408 |
| 2 | 1.328 | 22.141 | 82.549 |
| 3 | 0.520 | 8.671 | 91.220 |
| 4 | 0.336 | 5.594 | 96.814 |
| 5 | 0.125 | 2.090 | 98.904 |
| 6 | $6.578 \mathrm{E}-02$ | 1.096 | 100.00 |

Table 2
Principal Components for Efficiency Scores across Different TechniquesComponents Matrix

| Technique | Component 1 | Component 2 |
| :--- | :---: | :---: |
| DEA | 0.797 | 0.258 |
| DF-OLS | 0.657 | 0.583 |
| DF-RE | 0.912 | -0.208 |
| DF-SF-TN1 | 0.789 | -0.563 |
| DF-SF-TN2 | 0.842 | -0.415 |
| DF-SF-TN3 | 0.629 | 0.625 |

Table 3
Spearman Rank-Order Correlations Among the Efficiency Scores Created by Different Approaches

|  | DEA | DF-OLS | DF-RE | DF-SF-TN1 | DF-SF-TN2 | DF-SF-TN3 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| DEA | 1.000 | 0.580 | 0.540 | 0.443 | 0.597 | 0.649 |
|  |  | $(0.000)$ | $(0.000)$ | $(0.000)$ | $(0.000)$ | $(0.000)$ |
| DF-OLS |  | 1.000 | 0.585 | 0.278 | 0.372 | 0.767 |
|  |  |  | $(0.000)$ | $(0.000)$ | $(0.000)$ | $(0.000)$ |
| DF-RE |  |  | 1.000 | 0.849 | 0.826 | 0.440 |
|  |  |  |  | $(0.000)$ | $(0.000)$ | $(0.000)$ |
| DF-SF-TN1 |  |  |  | 1.000 | 0.852 | 0.177 |
|  |  |  |  |  | $(0.000)$ | $(0.000)$ |
| DF-SF-TN2 |  |  |  |  | 1.000 | 0.517 |
|  |  |  |  |  |  | $(0.000)$ |
| DF-SF-TN3 |  |  |  |  |  | 1.000 |

Note: the p-values are reported in parentheses for the non-trivial correlations

Table 4
Correspondence of Best Practice and Worst Practice LECs across Techniques (Upper triangle shows best practice, and lower triangle shows worst practice)

|  | DEA | DF-OLS | DF-RE | DF-SF-TN1 | DF-SF-TN2 | DF-SF-TN3 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| DEA |  | 0.423 | 0.474 | 0.487 | 0.513 | 0.385 |
| DF-OLS | 0.500 |  | 0.551 | 0.372 | 0.359 | 0.770 |
| DF-RE | 0.410 | 0.474 |  | 0.756 | 0.718 | 0.423 |
| DF-SF-TN1 | 0.500 | 0.333 | 0.718 |  | 0.692 | 0.244 |
| DF-SF-TN2 | 0.551 | 0.320 | 0.667 | 0.744 |  | 0.462 |
| DF-SF-TN3 | 0.551 | 0.513 | 0.308 | 0.333 | 0.372 |  |

Note: one considered the upper and lower $20 \%$ of the distribution

Table 5
Persistence of Efficiency-Correlations of $n$ Years Apart Efficiencies

| Technique | 1 year apart | $\begin{gathered} 2 \text { years } \\ \text { apart } \\ \hline \end{gathered}$ | 3 years apart | $\begin{gathered} 4 \text { years } \\ \text { apart } \\ \hline \end{gathered}$ | 5 years apart | 6 years apart | $\begin{gathered} 7 \text { years } \\ \text { apart } \end{gathered}$ | 8 years apart | $\begin{gathered} 9 \text { years } \\ \text { apart } \\ \hline \end{gathered}$ | 10 years apart | 11 years apart | $\begin{gathered} 12 \text { years } \\ \text { apart } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DEA | $\begin{gathered} 0.857 \\ (1.000) \end{gathered}$ | $\begin{gathered} \hline 0.762 \\ (1.000) \end{gathered}$ | $\begin{gathered} \hline 0.726 \\ (1.000) \end{gathered}$ | $\begin{gathered} \hline 0.704 \\ (1.000) \end{gathered}$ | $\begin{gathered} \hline 0.707 \\ (1.000) \end{gathered}$ | $\begin{gathered} \hline 0.693 \\ (1.000) \end{gathered}$ | $\begin{gathered} 0.636 \\ (1.000) \end{gathered}$ | $\begin{gathered} 0.568 \\ (1.000) \end{gathered}$ | $\begin{gathered} 0.596 \\ (0.750) \\ (0.514) \end{gathered}$ | $\begin{gathered} 0.639 \\ (0.667) \\ (0.494) \end{gathered}$ | $\begin{gathered} 0.564 \\ (1.000) \end{gathered}$ | $\begin{gathered} 0.564 \\ (1.000) \end{gathered}$ |
| DF-OLS | $\begin{gathered} 0.582 \\ (0.833) \\ (0.526) \\ \hline \end{gathered}$ | $\begin{gathered} 0.549 \\ (0.364) \\ (0.357) \\ \hline \end{gathered}$ | $\begin{gathered} 0.526 \\ (0.300) \\ (0.249) \\ \hline \end{gathered}$ | $\begin{gathered} 0.409 \\ (0.333) \\ (0.274) \\ \hline \end{gathered}$ | $\begin{array}{\|c\|} \hline 0.269 \\ (0.375) \\ (0.291) \\ \hline \end{array}$ | $\begin{array}{\|c\|} \hline 0.432 \\ (0.286) \\ (0.227) \\ \hline \end{array}$ | $\begin{gathered} 0.422 \\ (0.167) \\ (0.209) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.329 \\ (0.200) \\ (0.160) \end{gathered}$ | $\begin{gathered} 0.000 \\ (0.000) \end{gathered}$ | $\begin{gathered} 0.000 \\ (0.000) \end{gathered}$ | $\begin{gathered} 0.000 \\ (0.000) \end{gathered}$ | $\begin{gathered} 0.000 \\ (0.000) \end{gathered}$ |
| DF-RE | 0.911 | 0.870 | 0.844 | 0.838 | 0.823 | 0.820 | 0.804 | 0.776 | 0.733 | 0.733 | 0.737 | 0.733 |
| DF-SF-TN2 | 0.999 | 0.999 | 0.998 | 0.997 | 0.995 | 0.994 | 0.991 | 0.988 | 0.986 | 0.982 | 0.978 | 0.974 |
| DF-SF-TN3 | $\begin{gathered} 0.711 \\ (0.750) \end{gathered}$ | $\begin{gathered} 0.542 \\ (0.636) \end{gathered}$ | $\begin{gathered} 0.642 \\ (0.200) \end{gathered}$ | $\begin{gathered} 0.398 \\ (0.556) \\ (0.289) \end{gathered}$ | $\begin{gathered} 0.429 \\ (0.625) \end{gathered}$ $(0.299)$ | $\begin{array}{\|c\|} \hline 0.480 \\ (0.714) \\ (0.394) \end{array}$ | $\begin{gathered} 0.485 \\ (0.500) \\ (0.400) \end{gathered}$ | $\begin{gathered} 0.407 \\ (0.600) \end{gathered}$ (0.322) | $\begin{gathered} 0.508 \\ (0.250) \\ (0.198) \end{gathered}$ | $\begin{gathered} 0.370 \\ (0.333) \end{gathered}$ (0.190) | $\begin{gathered} 0.000 \\ (0.000) \end{gathered}$ | $\begin{gathered} 0.000 \\ (0.000) \end{gathered}$ |

Notes:
a) The first value in each cell of the table corresponds to the average of the correlations of the n-years-apart efficiencies.

The averages are computed over the 13-n correlations in each case, considering the ones that were significant at the $10 \%$ level
b)The first term in parentheses represents the proportion of cases that were significant at the $10 \%$ level, whereas the second term in parentheses indicates the average of all correlations

## Appendix 1

List of local exchange carriers-LECs

1) Bell-IL: Illinois Bell Telephone Company
2) Bell-IN: Indiana Bell Telephone Company

3 )Bell-MI: Michigan Bell Telephone Company
4) Bell-OH: Ohio Bell Telephone Company

5 )Bell-WI: Wisconsin Bell Inc.
6 )Ver-DC: Verizon Washington D.C. Inc.
7 )Ver-MD: Verzon Maryland
8) Ver-VA: Verzon Virginia
9) Ver-WV: Verzon West Virginia
10) Ver-DE: Verizon Delaware
11) Ver-PA: Verizon Pennsylvania
12) Ver-NJ: Verizon New Jersey
13) Ver-NE: Verizon New England
14) Ver-NY: Verizon New York
15) Nev. Bell: Nevada Bell
16) Pac. Bell. Pacific Bell
17) SW Bell. Southwestern Bell Telephone Company
18) Cinc. Bell: Cincinatti Bell Telephone Compoany
19) SNE: Southern New England Telephone Company
20) Centel-VA: Central Telephone Company of Virginia
21) Ver-CA: Verizon Califórnia Inc.
22) Ver-FL: Verizon Florida Inc.
23) Ver-HI: Verizon Hawaii Inc.
24) Ver-NO: Verizon North Inc.
25) Ver-NW: Verizon Northwest Inc.
26) Ver-SO: Verizon South Inc.
27) PR-Telco: Puerto Rico telephone Company
28) UT-IN: United Telephone Company of Indiana
29) UT-OH: United Telephone Company of Ohio
30) UT-PA:: United Telephone Company of Pennsylvania

## APPENDIX 2

Table A1-Efficiency Scores-Data Envelopment Analysis-BCC model-output orientation

|  | 1988 | 1989 | 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 | 1997 | 1998 | 1999 | 2000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bell-IL | 0.817 | 0.882 | 0.953 | 0.885 | 0.901 | 0.943 | 0.978 | 0.987 | 1.000 | 0.991 | 1.000 | 1.000 | 0.961 |
| Bell-IN | 0.620 | 0.601 | 0.605 | 0.599 | 0.703 | 0.717 | 0.784 | 0.841 | 0.912 | 0.930 | 0.979 | 1.000 | 0.964 |
| Bell-MI | 0.692 | 0.708 | 0.751 | 0.726 | 0.699 | 0.672 | 0.760 | 0.759 | 0.834 | 0.778 | 0.797 | 0.884 | 0.863 |
| Bell-OH | 0.733 | 0.719 | 0.729 | 0.775 | 0.785 | 0.825 | 0.843 | 0.947 | 1.000 | 0.987 | 1.000 | 1.000 | 0.954 |
| Bell-WI | 0.564 | 0.542 | 0.516 | 0.545 | 0.552 | 0.607 | 0.658 | 0.710 | 0.777 | 0.793 | 0.911 | 0.957 | 1.000 |
| Ver-DC | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 0.995 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| Ver-MD | 0.726 | 0.754 | 0.736 | 0.731 | 0.773 | 0.779 | 0.835 | 0.982 | 1.000 | 0.990 | 0.982 | 0.997 | 0.904 |
| Ver-VA | 0.718 | 0.675 | 0.695 | 0.690 | 0.742 | 0.727 | 0.721 | 0.902 | 0.976 | 0.988 | 1.000 | 1.000 | 0.947 |
| Ver-WV | 0.413 | 0.416 | 0.436 | 0.449 | 0.484 | 0.468 | 0.539 | 0.730 | 0.762 | 0.760 | 0.805 | 0.805 | 0.852 |
| Ver-DE | 1.000 | 1.000 | 1.000 | 0.827 | 0.815 | 0.735 | 0.711 | 0.847 | 1.000 | 0.978 | 1.000 | 1.000 | 0.993 |
| Ver-PA | 0.732 | 0.727 | 0.752 | 0.746 | 0.755 | 0.740 | 0.771 | 0.887 | 0.946 | 0.936 | 0.970 | 1.000 | 0.961 |
| Ver-NJ | 0.800 | 0.766 | 0.810 | 0.785 | 0.750 | 0.758 | 0.774 | 0.850 | 0.932 | 1.000 | 0.981 | 1.000 | 1.000 |
| Ver-NE | 0.654 | 0.568 | 0.557 | 0.540 | 0.570 | 0.604 | 0.568 | 0.715 | 0.592 | 0.588 | 0.711 | 0.777 | 0.827 |
| Ver-NY | 0.639 | 0.578 | 0.617 | 0.603 | 0.632 | 0.646 | 0.684 | 0.715 | 0.742 | 0.752 | 0.761 | 1.000 | 0.981 |
| Nev. Bell | 1.000 | 1.000 | 1.000 | 0.854 | 0.830 | 0.933 | 1.000 | 1.000 | 1.000 | 0.955 | 1.000 | 1.000 | 0.767 |
| Pac. Bell | 0.777 | 0.776 | 0.795 | 1.000 | 0.901 | 0.921 | 0.922 | 0.936 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| SW Bell | 0.855 | 0.927 | 0.935 | 0.966 | 0.952 | 0.932 | 0.970 | 0.999 | 1.000 | 0.983 | 1.000 | 1.000 | 1.000 |
| Cinc. Bell | 0.696 | 0.696 | 0.631 | 0.635 | 0.637 | 0.663 | 0.709 | 0.749 | 0.829 | 1.000 | 0.898 | 0.955 | 0.960 |
| SNE | 0.512 | 0.504 | 0.511 | 0.498 | 0.525 | 0.541 | 0.540 | 0.554 | 0.667 | 0.670 | 0.679 | 0.529 | 0.617 |
| Centel-VA | 1.000 | 0.721 | 0.727 | 0.807 | 0.691 | 0.680 | 0.628 | 0.756 | 0.980 | 1.000 | 1.000 | 1.000 | 1.000 |
| Ver-CA | 1.000 | 0.773 | 0.568 | 0.612 | 0.795 | 0.692 | 0.694 | 0.850 | 0.668 | 0.721 | 0.754 | 0.879 | 1.000 |
| Ver-FL | 0.522 | 0.404 | 0.471 | 0.506 | 0.599 | 0.586 | 0.504 | 0.801 | 0.694 | 0.795 | 0.736 | 0.822 | 0.697 |
| Ver-HI | 0.641 | 1.000 | 0.597 | 0.577 | 0.597 | 0.582 | 0.575 | 0.603 | 0.581 | 0.641 | 0.666 | 0.746 | 0.888 |
| Ver-NO | 0.499 | 0.466 | 0.475 | 0.501 | 0.569 | 0.570 | 0.579 | 0.636 | 0.617 | 0.682 | 0.650 | 0.879 | 1.000 |
| Ver-NW | 0.380 | 0.059 | 0.365 | 0.388 | 0.418 | 0.415 | 0.435 | 0.641 | 0.596 | 0.661 | 0.785 | 0.837 | 0.800 |
| Ver-SO | 0.299 | 0.251 | 0.330 | 0.347 | 0.408 | 0.445 | 0.465 | 0.605 | 0.603 | 0.635 | 0.671 | 0.745 | 1.000 |
| PR Telco | 0.438 | 0.594 | 0.534 | 0.605 | 0.643 | 0.535 | 0.504 | 0.453 | 0.622 | 0.659 | 0.722 | 0.720 | 0.780 |
| UT-IN | 1.000 | 0.851 | 0.679 | 1.000 | 0.692 | 0.507 | 0.614 | 0.673 | 1.000 | 1.000 | 1.000 | 0.876 | 1.000 |
| UT-OH | 0.298 | 0.280 | 0.427 | 0.512 | 0.496 | 0.444 | 0.461 | 0.469 | 0.691 | 0.669 | 0.716 | 0.583 | 0.635 |
| UT-PA | 0.467 | 0.345 | 1.000 | 1.000 | 0.458 | 0.368 | 0.415 | 0.407 | 0.775 | 0.732 | 0.605 | 0.570 | 0.646 |

Table A2 - Efficiency Scores-Input Distance Function-(corrected) ordinary least squares model

|  | 1988 | 1989 | 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 | 1997 | 1998 | 1999 | 2000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bell-IL | 0.634 | 0.622 | 0.802 | 0.554 | 0.539 | 0.556 | 0.608 | 0.537 | 0.603 | 0.603 | 0.609 | 0.610 | 0.553 |
| Bell-IN | 0.498 | 0.458 | 0.450 | 0.419 | 0.472 | 0.512 | 0.527 | 0.519 | 0.640 | 0.612 | 0.602 | 0.599 | 0.548 |
| Bell-MI | 0.426 | 0.421 | 0.437 | 0.424 | 0.399 | 0.372 | 0.512 | 0.401 | 0.455 | 0.418 | 0.380 | 0.422 | 0.358 |
| Bell-OH | 0.531 | 0.505 | 0.504 | 0.520 | 0.492 | 0.504 | 0.550 | 0.507 | 0.592 | 0.561 | 0.542 | 0.567 | 0.479 |
| Bell-WI | 0.445 | 0.442 | 0.390 | 0.382 | 0.369 | 0.383 | 0.432 | 0.455 | 0.489 | 0.466 | 0.429 | 0.441 | 0.398 |
| Ver-DC | 0.514 | 0.449 | 0.649 | 0.582 | 0.598 | 0.571 | 0.593 | 0.457 | 0.421 | 0.451 | 0.465 | 0.418 | 0.418 |
| Ver-MD | 0.498 | 0.516 | 0.530 | 0.483 | 0.518 | 0.512 | 0.538 | 0.565 | 0.566 | 0.571 | 0.609 | 0.639 | 0.627 |
| Ver-VA | 0.480 | 0.460 | 0.497 | 0.451 | 0.486 | 0.457 | 0.444 | 0.463 | 0.473 | 0.484 | 0.491 | 0.512 | 0.500 |
| Ver-WV | 0.368 | 0.422 | 0.414 | 0.410 | 0.445 | 0.410 | 0.433 | 0.487 | 0.508 | 0.590 | 0.598 | 0.612 | 0.611 |
| Ver-DE | 0.391 | 0.370 | 0.478 | 0.472 | 0.470 | 0.460 | 0.477 | 0.508 | 0.581 | 0.666 | 0.731 | 0.693 | 0.598 |
| Ver-PA | 0.475 | 0.485 | 0.532 | 0.494 | 0.496 | 0.491 | 0.494 | 0.498 | 0.519 | 0.560 | 0.566 | 0.598 | 0.527 |
| Ver-NJ | 0.499 | 0.409 | 0.493 | 0.489 | 0.452 | 0.461 | 0.560 | 0.431 | 0.483 | 0.505 | 0.611 | 0.665 | 0.672 |
| Ver-NE | 0.443 | 0.400 | 0.397 | 0.366 | 0.396 | 0.421 | 0.328 | 0.382 | 0.293 | 0.288 | 0.361 | 0.417 | 0.398 |
| Ver-NY | 0.358 | 0.351 | 0.410 | 0.369 | 0.437 | 0.427 | 0.358 | 0.362 | 0.416 | 0.410 | 0.396 | 0.507 | 0.517 |
| Nev. Bell | 0.455 | 0.384 | 0.426 | 0.417 | 0.424 | 0.407 | 0.539 | 0.523 | 0.477 | 0.514 | 0.445 | 0.623 | 0.403 |
| Pac. Bell | 0.433 | 0.444 | 0.468 | 1.000 | 0.538 | 0.573 | 0.536 | 0.526 | 0.674 | 0.560 | 0.599 | 0.519 | 0.457 |
| SW Bell | 0.412 | 0.453 | 0.457 | 0.460 | 0.494 | 0.446 | 0.463 | 0.471 | 0.559 | 0.583 | 0.575 | 0.533 | 0.525 |
| Cinc. Bell | 0.422 | 0.423 | 0.376 | 0.405 | 0.423 | 0.458 | 0.502 | 0.392 | 0.580 | 0.745 | 0.543 | 0.591 | 0.596 |
| SNE | 0.363 | 0.362 | 0.368 | 0.339 | 0.437 | 0.444 | 0.407 | 0.378 | 0.520 | 0.460 | 0.411 | 0.294 | 0.258 |
| Centel-VA | 0.587 | 0.504 | 0.487 | 0.479 | 0.486 | 0.498 | 0.441 | 0.483 | 0.495 | 0.569 | 0.443 | 0.334 | 0.365 |
| Ver-CA | 0.732 | 0.542 | 0.450 | 0.489 | 0.608 | 0.546 | 0.503 | 0.509 | 0.517 | 0.520 | 0.543 | 0.668 | 0.894 |
| Ver-FL | 0.257 | 0.271 | 0.401 | 0.498 | 0.607 | 0.563 | 0.199 | 0.617 | 0.636 | 0.773 | 0.620 | 0.727 | 0.536 |
| Ver-HI | 0.399 | 0.726 | 0.455 | 0.461 | 0.475 | 0.440 | 0.378 | 0.360 | 0.399 | 0.481 | 0.448 | 0.592 | 0.703 |
| Ver-NO | 0.570 | 0.477 | 0.422 | 0.361 | 0.405 | 0.393 | 0.381 | 0.351 | 0.385 | 0.422 | 0.377 | 0.570 | 0.714 |
| Ver-NW | 0.422 | 0.295 | 0.421 | 0.525 | 0.427 | 0.389 | 0.404 | 0.360 | 0.476 | 0.538 | 0.526 | 0.783 | 0.633 |
| Ver-SO | 0.294 | 0.355 | 0.410 | 0.428 | 0.433 | 0.412 | 0.438 | 0.334 | 0.459 | 0.486 | 0.520 | 0.626 | 0.902 |
| PR Telco | 0.284 | 0.462 | 0.428 | 0.430 | 0.483 | 0.902 | 0.410 | 0.391 | 0.389 | 0.406 | 0.447 | 0.457 | 0.536 |
| UT-IN | 0.712 | 0.644 | 0.552 | 0.492 | 0.427 | 0.348 | 0.351 | 0.371 | 0.610 | 0.535 | 0.555 | 0.382 | 0.487 |
| UT-OH | 0.333 | 0.308 | 0.534 | 0.571 | 0.516 | 0.471 | 0.471 | 0.467 | 0.707 | 0.667 | 0.649 | 0.394 | 0.437 |
| UT-PA | 0.400 | 0.267 | 0.518 | 0.508 | 0.405 | 0.333 | 0.368 | 0.358 | 0.623 | 0.593 | 0.454 | 0.309 | 0.386 |

Table A3 - Efficiency Scores-Input Distance Function-(corrected) random effects model

|  | 1988 | 1989 | 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 | 1997 | 1998 | 1999 | 2000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bell-IL | 0.713 | 0.714 | 0.848 | 0.663 | 0.643 | 0.660 | 0.664 | 0.633 | 0.676 | 0.671 | 0.662 | 0.648 | 0.612 |
| Bell-IN | 0.453 | 0.427 | 0.420 | 0.402 | 0.456 | 0.468 | 0.460 | 0.499 | 0.560 | 0.534 | 0.529 | 0.521 | 0.488 |
| Bell-MI | 0.386 | 0.382 | 0.405 | 0.393 | 0.374 | 0.350 | 0.424 | 0.363 | 0.378 | 0.356 | 0.328 | 0.337 | 0.301 |
| Bell-OH | 0.543 | 0.527 | 0.530 | 0.547 | 0.525 | 0.528 | 0.559 | 0.544 | 0.599 | 0.562 | 0.542 | 0.534 | 0.479 |
| Bell-WI | 0.447 | 0.450 | 0.414 | 0.411 | 0.400 | 0.417 | 0.441 | 0.453 | 0.470 | 0.441 | 0.417 | 0.431 | 0.399 |
| Ver-DC | 0.770 | 0.704 | 0.959 | 0.913 | 0.934 | 0.914 | 0.944 | 0.822 | 0.797 | 0.828 | 0.842 | 0.777 | 0.753 |
| Ver-MD | 0.524 | 0.579 | 0.579 | 0.530 | 0.547 | 0.553 | 0.580 | 0.613 | 0.611 | 0.592 | 0.612 | 0.639 | 0.633 |
| Ver-VA | 0.492 | 0.491 | 0.504 | 0.459 | 0.479 | 0.458 | 0.441 | 0.463 | 0.485 | 0.480 | 0.480 | 0.492 | 0.482 |
| Ver-WV | 0.304 | 0.366 | 0.343 | 0.349 | 0.373 | 0.348 | 0.358 | 0.408 | 0.417 | 0.448 | 0.453 | 0.448 | 0.443 |
| Ver-DE | 0.437 | 0.463 | 0.522 | 0.520 | 0.525 | 0.490 | 0.494 | 0.557 | 0.634 | 0.675 | 0.716 | 0.683 | 0.611 |
| Ver-PA | 0.442 | 0.530 | 0.562 | 0.518 | 0.518 | 0.510 | 0.502 | 0.510 | 0.521 | 0.540 | 0.544 | 0.567 | 0.505 |
| Ver-NJ | 0.653 | 0.567 | 0.678 | 0.651 | 0.582 | 0.590 | 0.652 | 0.544 | 0.595 | 0.631 | 0.711 | 0.765 | 0.775 |
| Ver-NE | 0.402 | 0.380 | 0.374 | 0.334 | 0.352 | 0.368 | 0.314 | 0.357 | 0.269 | 0.269 | 0.336 | 0.372 | 0.356 |
| Ver-NY | 0.461 | 0.476 | 0.565 | 0.503 | 0.562 | 0.552 | 0.486 | 0.485 | 0.557 | 0.559 | 0.541 | 0.694 | 0.703 |
| Nev. Bell | 0.437 | 0.395 | 0.414 | 0.407 | 0.412 | 0.402 | 0.499 | 0.497 | 0.478 | 0.489 | 0.512 | 0.634 | 0.438 |
| Pac. Bell | 0.559 | 0.563 | 0.586 | 1.000 | 0.644 | 0.675 | 0.634 | 0.620 | 0.723 | 0.674 | 0.704 | 0.652 | 0.602 |
| SW Bell | 0.332 | 0.366 | 0.376 | 0.358 | 0.365 | 0.365 | 0.370 | 0.374 | 0.453 | 0.482 | 0.480 | 0.468 | 0.456 |
| Cinc. Bell | 0.551 | 0.609 | 0.545 | 0.556 | 0.565 | 0.593 | 0.640 | 0.567 | 0.716 | 0.958 | 0.724 | 0.752 | 0.707 |
| SNE | 0.412 | 0.408 | 0.414 | 0.388 | 0.498 | 0.505 | 0.466 | 0.439 | 0.565 | 0.490 | 0.442 | 0.306 | 0.300 |
| Centel-VA | 0.333 | 0.302 | 0.289 | 0.283 | 0.298 | 0.304 | 0.277 | 0.296 | 0.321 | 0.349 | 0.281 | 0.256 | 0.263 |
| Ver-CA | 0.828 | 0.680 | 0.506 | 0.551 | 0.655 | 0.581 | 0.549 | 0.575 | 0.510 | 0.523 | 0.542 | 0.610 | 0.801 |
| Ver-FL | 0.333 | 0.310 | 0.410 | 0.488 | 0.562 | 0.537 | 0.279 | 0.571 | 0.589 | 0.705 | 0.633 | 0.700 | 0.564 |
| Ver-HI | 0.486 | 0.582 | 0.517 | 0.516 | 0.531 | 0.517 | 0.469 | 0.442 | 0.478 | 0.550 | 0.545 | 0.632 | 0.746 |
| Ver-NO | 0.229 | 0.200 | 0.195 | 0.168 | 0.178 | 0.173 | 0.168 | 0.151 | 0.165 | 0.173 | 0.167 | 0.217 | 0.289 |
| Ver-NW | 0.368 | 0.213 | 0.339 | 0.380 | 0.322 | 0.287 | 0.299 | 0.268 | 0.339 | 0.391 | 0.387 | 0.530 | 0.453 |
| Ver-SO | 0.159 | 0.225 | 0.258 | 0.260 | 0.255 | 0.303 | 0.210 | 0.185 | 0.243 | 0.261 | 0.284 | 0.329 | 0.484 |
| PR Telco | 0.321 | 0.413 | 0.387 | 0.380 | 0.427 | 0.677 | 0.367 | 0.349 | 0.363 | 0.382 | 0.402 | 0.438 | 0.473 |
| UT-IN | 0.411 | 0.379 | 0.299 | 0.269 | 0.252 | 0.223 | 0.228 | 0.242 | 0.360 | 0.326 | 0.321 | 0.254 | 0.300 |
| UT-OH | 0.200 | 0.189 | 0.315 | 0.336 | 0.318 | 0.298 | 0.299 | 0.299 | 0.416 | 0.395 | 0.391 | 0.277 | 0.296 |
| UT-PA | 0.247 | 0.181 | 0.310 | 0.303 | 0.254 | 0.223 | 0.242 | 0.241 | 0.370 | 0.350 | 0.288 | 0.223 | 0.256 |

Table A4 - Efficiency Scores-Output Distance Function-Normal/Half Normal model-Time Invariant Efficiencies

|  | 1988 | 1989 | 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 | 1997 | 1998 | 1999 | 2000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bell-IL | 0.663 | 0.663 | 0.663 | 0.663 | 0.663 | 0.663 | 0.663 | 0.663 | 0.663 | 0.663 | 0.663 | 0.663 | 0.663 |
| Bell-IN | 0.497 | 0.497 | 0.497 | 0.497 | 0.497 | 0.497 | 0.497 | 0.497 | 0.497 | 0.497 | 0.497 | 0.497 | 0.497 |
| Bell-MI | 0.402 | 0.402 | 0.402 | 0.402 | 0.402 | 0.402 | 0.402 | 0.402 | 0.402 | 0.402 | 0.402 | 0.402 | 0.402 |
| Bell-OH | 0.580 | 0.580 | 0.580 | 0.580 | 0.580 | 0.580 | 0.580 | 0.580 | 0.580 | 0.580 | 0.580 | 0.580 | 0.580 |
| Bell-WI | 0.520 | 0.520 | 0.520 | 0.520 | 0.520 | 0.520 | 0.520 | 0.520 | 0.520 | 0.520 | 0.520 | 0.520 | 0.520 |
| Ver-DC | 0.937 | 0.937 | 0.937 | 0.937 | 0.937 | 0.937 | 0.937 | 0.937 | 0.937 | 0.937 | 0.937 | 0.937 | 0.937 |
| Ver-MD | 0.608 | 0.608 | 0.608 | 0.608 | 0.608 | 0.608 | 0.608 | 0.608 | 0.608 | 0.608 | 0.608 | 0.608 | 0.608 |
| Ver-VA | 0.576 | 0.576 | 0.576 | 0.576 | 0.576 | 0.576 | 0.576 | 0.576 | 0.576 | 0.576 | 0.576 | 0.576 | 0.576 |
| Ver-WV | 0.336 | 0.336 | 0.336 | 0.336 | 0.336 | 0.336 | 0.336 | 0.336 | 0.336 | 0.336 | 0.336 | 0.336 | 0.336 |
| Ver-DE | 0.584 | 0.584 | 0.584 | 0.584 | 0.584 | 0.584 | 0.584 | 0.584 | 0.584 | 0.584 | 0.584 | 0.584 | 0.584 |
| Ver-PA | 0.540 | 0.540 | 0.540 | 0.540 | 0.540 | 0.540 | 0.540 | 0.540 | 0.540 | 0.540 | 0.540 | 0.540 | 0.540 |
| Ver-NJ | 0.888 | 0.888 | 0.888 | 0.888 | 0.888 | 0.888 | 0.888 | 0.888 | 0.888 | 0.888 | 0.888 | 0.888 | 0.888 |
| Ver-NE | 0.368 | 0.368 | 0.368 | 0.368 | 0.368 | 0.368 | 0.368 | 0.368 | 0.368 | 0.368 | 0.368 | 0.368 | 0.368 |
| Ver-NY | 0.548 | 0.548 | 0.548 | 0.548 | 0.548 | 0.548 | 0.548 | 0.548 | 0.548 | 0.548 | 0.548 | 0.548 | 0.548 |
| Nev. Bell | 0.390 | 0.390 | 0.390 | 0.390 | 0.390 | 0.390 | 0.390 | 0.390 | 0.390 | 0.390 | 0.390 | 0.390 | 0.390 |
| Pac. Bell | 0.585 | 0.585 | 0.585 | 0.585 | 0.585 | 0.585 | 0.585 | 0.585 | 0.585 | 0.585 | 0.585 | 0.585 | 0.585 |
| SW Bell | 0.335 | 0.335 | 0.335 | 0.335 | 0.335 | 0.335 | 0.335 | 0.335 | 0.335 | 0.335 | 0.335 | 0.335 | 0.335 |
| Cinc. Bell | 0.630 | 0.630 | 0.630 | 0.630 | 0.630 | 0.630 | 0.630 | 0.630 | 0.630 | 0.630 | 0.630 | 0.630 | 0.630 |
| SNE | 0.438 | 0.438 | 0.438 | 0.438 | 0.438 | 0.438 | 0.438 | 0.438 | 0.438 | 0.438 | 0.438 | 0.438 | 0.438 |
| Centel-VA | 0.240 | 0.240 | 0.240 | 0.240 | 0.240 | 0.240 | 0.240 | 0.240 | 0.240 | 0.240 | 0.240 | 0.240 | 0.240 |
| Ver-CA | 0.490 | 0.490 | 0.490 | 0.490 | 0.490 | 0.490 | 0.490 | 0.490 | 0.490 | 0.490 | 0.490 | 0.490 | 0.490 |
| Ver-FL | 0.436 | 0.436 | 0.436 | 0.436 | 0.436 | 0.436 | 0.436 | 0.436 | 0.436 | 0.436 | 0.436 | 0.436 | 0.436 |
| Ver-HI | 0.396 | 0.396 | 0.396 | 0.396 | 0.396 | 0.396 | 0.396 | 0.396 | 0.396 | 0.396 | 0.396 | 0.396 | 0.396 |
| Ver-NO | 0.152 | 0.152 | 0.152 | 0.152 | 0.152 | 0.152 | 0.152 | 0.152 | 0.152 | 0.152 | 0.152 | 0.152 | 0.152 |
| Ver-NW | 0.280 | 0.280 | 0.280 | 0.280 | 0.280 | 0.280 | 0.280 | 0.280 | 0.280 | 0.280 | 0.280 | 0.280 | 0.280 |
| Ver-SO | 0.224 | 0.224 | 0.224 | 0.224 | 0.224 | 0.224 | 0.224 | 0.224 | 0.224 | 0.224 | 0.224 | 0.224 | 0.224 |
| PR Telco | 0.222 | 0.222 | 0.222 | 0.222 | 0.222 | 0.222 | 0.222 | 0.222 | 0.222 | 0.222 | 0.222 | 0.222 | 0.222 |
| UT-IN | 0.198 | 0.198 | 0.198 | 0.198 | 0.198 | 0.198 | 0.198 | 0.198 | 0.198 | 0.198 | 0.198 | 0.198 | 0.198 |
| UT-OH | 0.206 | 0.206 | 0.206 | 0.206 | 0.206 | 0.206 | 0.206 | 0.206 | 0.206 | 0.206 | 0.206 | 0.206 | 0.206 |
| UT-PA | 0.175 | 0.175 | 0.175 | 0.175 | 0.175 | 0.175 | 0.175 | 0.175 | 0.175 | 0.175 | 0.175 | 0.175 | 0.175 |

Table A5 - Efficiency Scores-Output Distance Function- Normal/Half Normal model-Time Varying Efficiencies

|  | 1988 | 1989 | 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 | 1997 | 1998 | 1999 | 2000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bell-IL | 0.306 | 0.322 | 0.339 | 0.356 | 0.372 | 0.389 | 0.405 | 0.422 | 0.438 | 0.455 | 0.471 | 0.487 | 0.502 |
| Bell-IN | 0.181 | 0.195 | 0.210 | 0.225 | 0.240 | 0.256 | 0.272 | 0.288 | 0.304 | 0.321 | 0.337 | 0.354 | 0.370 |
| Bell-MI | 0.156 | 0.170 | 0.183 | 0.198 | 0.212 | 0.227 | 0.243 | 0.258 | 0.274 | 0.290 | 0.307 | 0.323 | 0.340 |
| Bell-OH | 0.234 | 0.249 | 0.265 | 0.281 | 0.297 | 0.314 | 0.330 | 0.347 | 0.363 | 0.380 | 0.397 | 0.413 | 0.430 |
| Bell-WI | 0.187 | 0.202 | 0.217 | 0.232 | 0.247 | 0.263 | 0.279 | 0.295 | 0.312 | 0.328 | 0.345 | 0.361 | 0.378 |
| Ver-DC | 0.937 | 0.940 | 0.942 | 0.945 | 0.947 | 0.949 | 0.952 | 0.954 | 0.956 | 0.958 | 0.959 | 0.961 | 0.963 |
| Ver-MD | 0.245 | 0.261 | 0.277 | 0.292 | 0.309 | 0.327 | 0.342 | 0.359 | 0.376 | 0.392 | 0.409 | 0.425 | 0.442 |
| Ver-VA | 0.221 | 0.236 | 0.252 | 0.268 | 0.284 | 0.300 | 0.316 | 0.333 | 0.350 | 0.366 | 0.383 | 0.399 | 0.416 |
| Ver-WV | 0.105 | 0.116 | 0.128 | 0.140 | 0.152 | 0.166 | 0.179 | 0.193 | 0.208 | 0.223 | 0.238 | 0.254 | 0.270 |
| Ver-DE | 0.202 | 0.216 | 0.231 | 0.247 | 0.262 | 0.279 | 0.295 | 0.311 | 0.328 | 0.344 | 0.361 | 0.377 | 0.394 |
| Ver-PA | 0.228 | 0.243 | 0.259 | 0.275 | 0.291 | 0.307 | 0.324 | 0.340 | 0.357 | 0.374 | 0.390 | 0.407 | 0.423 |
| Ver-NJ | 0.374 | 0.390 | 0.407 | 0.423 | 0.440 | 0.456 | 0.472 | 0.488 | 0.504 | 0.519 | 0.534 | 0.549 | 0.564 |
| Ver-NE | 0.152 | 0.165 | 0.179 | 0.193 | 0.208 | 0.223 | 0.238 | 0.264 | 0.269 | 0.286 | 0.302 | 0.318 | 0.335 |
| Ver-NY | 0.261 | 0.277 | 0.293 | 0.309 | 0.326 | 0.342 | 0.359 | 0.376 | 0.392 | 0.409 | 0.425 | 0.442 | 0.458 |
| Nev. Bell | 0.139 | 0.151 | 0.164 | 0.178 | 0.192 | 0.207 | 0.222 | 0.237 | 0.252 | 0.268 | 0.284 | 0.301 | 0.317 |
| Pac. Bell | 0.302 | 0.319 | 0.335 | 0.352 | 0.368 | 0.385 | 0.402 | 0.418 | 0.435 | 0.451 | 0.467 | 0.483 | 0.499 |
| SW Bell | 0.156 | 0.170 | 0.183 | 0.198 | 0.212 | 0.227 | 0.243 | 0.258 | 0.274 | 0.290 | 0.307 | 0.323 | 0.340 |
| Cinc. Bell | 0.250 | 0.266 | 0.282 | 0.298 | 0.315 | 0.331 | 0.348 | 0.364 | 0.381 | 0.397 | 0.414 | 0.430 | 0.447 |
| SNE | 0.159 | 0.173 | 0.187 | 0.201 | 0.216 | 0.231 | 0.246 | 0.262 | 0.278 | 0.294 | 0.311 | 0.327 | 0.344 |
| Centel-VA | 0.072 | 0.081 | 0.091 | 0.101 | 0.112 | 0.123 | 0.135 | 0.148 | 0.160 | 0.174 | 0.188 | 0.202 | 0.217 |
| Ver-CA | 0.219 | 0.234 | 0.250 | 0.266 | 0.282 | 0.298 | 0.314 | 0.331 | 0.347 | 0.364 | 0.381 | 0.397 | 0.414 |
| Ver-FL | 0.164 | 0.178 | 0.192 | 0.207 | 0.222 | 0.237 | 0.252 | 0.268 | 0.284 | 0.301 | 0.317 | 0.334 | 0.350 |
| Ver-HI | 0.174 | 0.188 | 0.202 | 0.217 | 0.232 | 0.248 | 0.263 | 0.279 | 0.296 | 0.312 | 0.328 | 0.345 | 0.362 |
| Ver-NO | 0.052 | 0.059 | 0.067 | 0.075 | 0.084 | 0.094 | 0.105 | 0.116 | 0.127 | 0.139 | 0.152 | 0.165 | 0.179 |
| Ver-NW | 0.087 | 0.096 | 0.107 | 0.118 | 0.130 | 0.142 | 0.155 | 0.168 | 0.182 | 0.196 | 0.211 | 0.226 | 0.241 |
| Ver-SO | 0.067 | 0.075 | 0.084 | 0.094 | 0.104 | 0.116 | 0.127 | 0.139 | 0.152 | 0.165 | 0.179 | 0.193 | 0.207 |
| PR Telco | 0.083 | 0.093 | 0.103 | 0.114 | 0.126 | 0.138 | 0.150 | 0.163 | 0.177 | 0.191 | 0.206 | 0.220 | 0.236 |
| UT-IN | 0.057 | 0.064 | 0.073 | 0.081 | 0.091 | 0.102 | 0.112 | 0.124 | 0.136 | 0.148 | 0.161 | 0.175 | 0.189 |
| UT-OH | 0.054 | 0.061 | 0.069 | 0.078 | 0.087 | 0.097 | 0.107 | 0.118 | 0.130 | 0.142 | 0.155 | 0.169 | 0.182 |
| UT-PA | 0.044 | 0.051 | 0.058 | 0.066 | 0.074 | 0.083 | 0.093 | 0.103 | 0.114 | 0.126 | 0.138 | 0.150 | 0.163 |

Table A6 - Efficiency Scores-Input Distance Function- Normal/Half Normal model- with Inefficiency Effects

|  | 1988 | 1989 | 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 | 1997 | 1998 | 1999 | 2000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bell-IL | 0.908 | 0.916 | 0.947 | 0.914 | 0.919 | 0.930 | 0.943 | 0.937. | 0.952 | 0.955 | 0.959 | 0.962 | 0.959 |
| Bell-IN | 0.851 | 0.838 | 0.852 | 0.850 | 0.898 | 0.922 | 0.926 | 0.934 | 0.956 | 0.956 | 0.958 | 0.960 | 0.959 |
| Bell-MI | 0.800 | 0.814 | 0.846 | 0.855 | 0.852 | 0.846 | 0.922 | 0.896 | 0.929 | 0.925 | 0.920 | 0.940 | 0.928 |
| Bell-OH | 0.874 | 0.874 | 0.887 | 0.908 | 0.907 | 0.920 | 0.933 | 0.932 | 0.951 | 0.951 | 0.952 | 0.959 | 0.951 |
| Bell-WI | 0.800 | 0.821 | 0.794 | 0.816 | 0.823 | 0.856 | 0.898 | 0.921 | 0.937 | 0.938 | 0.937 | 0.944 | 0.941 |
| Ver-DC | 0.878 | 0.860 | 0.939 | 0.930 | 0.937 | 0.936 | 0.944 | 0.924 | 0.921 | 0.935 | 0.942 | 0.934 | 0.937 |
| Ver-MD | 0.838 | 0.861 | 0.906 | 0.894 | 0.918 | 0.923 | 0.934 | 0.944 | 0.948 | 0.953 | 0.959 | 0.963 | 0.964 |
| Ver-VA | 0.822 | 0.825 | 0.899 | 0.885 | 0.913 | 0.910 | 0.913 | 0.926 | 0.933 | 0.941 | 0.948 | 0.954 | 0.955 |
| Ver-WV | 0.668 | 0.753 | 0.819 | 0.832 | 0.877 | 0.866 | 0.897 | 0.926 | 0.937 | 0.954 | 0.957 | 0.961 | 0.963 |
| Ver-DE | 0.728 | 0.710 | 0.874 | 0.887 | 0.900 | 0.904 | 0.919 | 0.935 | 0.951 | 0.961 | 0.967 | 0.967 | 0.963 |
| Ver-PA | 0.840 | 0.836 | 0.908 | 0.899 | 0.908 | 0.915 | 0.924 | 0.931 | 0.941 | 0.951 | 0.956 | 0.961 | 0.957 |
| Ver-NJ | 0.830 | 0.760 | 0.875 | 0.887 | 0.885 | 0.901 | 0.937 | 0.916 | 0.937 | 0.945 | 0.960 | 0.965 | 0.966 |
| Ver-NE | 0.827 | 0.798 | 0.814 | 0.802 | 0.850 | 0.883 | 0.814 | 0.881 | 0.816 | 0.830 | 0.904 | 0.935 | 0.935 |
| Ver-NY | 0.670 | 0.692 | 0.806 | 0.785 | 0.865 | 0.875 | 0.838 | 0.862 | 0.904 | 0.909 | 0.913 | 0.947 | 0.951 |
| Nev. Bell | 0.811 | 0.784 | 0.839 | 0.847 | 0.868 | 0.875 | 0.936 | 0.937 | 0.933 | 0.944 | 0.935 | 0.961 | 0.935 |
| Pac. Bell | 0.813 | 0.840 | 0.882 | 0.957 | 0.920 | 0.934 | 0.934 | 0.938 | 0.959 | 0.951 | 0.959 | 0.953 | 0.949 |
| SW Bell | 0.800 | 0.861 | 0.878 | 0.891 | 0.912 | 0.899 | 0.914 | 0.923 | 0.947 | 0.953 | 0.956 | 0.953 | 0.955 |
| Cinc. Bell | 0.760 | 0.744 | 0.710 | 0.783 | 0.844 | 0.888 | 0.916 | 0.875 | 0.945 | 0.962 | 0.947 | 0.955 | 0.958 |
| SNE | 0.641 | 0.680 | 0.719 | 0.701 | 0.834 | 0.860 | 0.854 | 0.859 | 0.924 | 0.925 | 0.918 | 0.861 | 0.843 |
| Centel-VA | 0.892 | 0.870 | 0.873 | 0.869 | 0.896 | 0.912 | 0.907 | 0.930 | 0.930 | 0.949 | 0.941 | 0.910 | 0.930 |
| Ver-CA | 0.914 | 0.864 | 0.876 | 0.894 | 0.935 | 0.929 | 0.924 | 0.932 | 0.940 | 0.944 | 0.951 | 0.964 | 0.974 |
| Ver-FL | 0.485 | 0.546 | 0.785 | 0.879 | 0.924 | 0.926 | 0.536 | 0.950 | 0.955 | 0.965 | 0.958 | 0.967 | 0.955 |
| Ver-HI | 0.728 | 0.929 | 0.862 | 0.882 | 0.897 | $0 . .889$ | 0.861 | 0.870 | 0.903 | 0.937 | 0.932 | 0.959 | 0.968 |
| Ver-NO | 0.849 | 0.810 | 0.846 | 0.798 | 0.859 | 0.867 | 0.873 | 0.868 | 0.901 | 0.925 | 0.914 | 0.958 | 0.969 |
| Ver-NW | 0.696 | 0.285 | 0.843 | 0.914 | 0.881 | 0.864 | 0.890 | 0.874 | 0.933 | 0.947 | 0.949 | 0.969 | 0.964 |
| Ver-SO | 0.586 | 0.611 | 0.842 | 0.861 | 0.873 | 0.882 | 0.894 | 0.835 | 0.921 | 0.933 | 0.942 | 0.957 | 0.972 |
| PR Telco | 0.388 | 0.785 | 0.780 | 0.850 | 0.892 | 0.957 | 0.897 | 0.882 | 0.909 | 0.922 | 0.942 | 0.944 | 0.958 |
| UT-IN | 0.918 | 0.912 | 0.914 | 0.905 | 0.887 | 0.836 | 0.860 | 0.889 | 0.957 | 0.952 | 0.954 | 0.926 | 0.953 |
| UT-OH | 0.646 | 0.634 | 0.883 | 0.913 | 0.905 | 0.905 | 0.918 | 0.925 | 0.961 | 0.962 | 0.958 | 0.927 | 0.943 |
| UT-PA | 0.669 | 0.505 | 0.880 | 0.890 | 0.845 | 0.801 | 0.861 | 0.868 | 0.953 | 0.955 | 0.932 | 0.885 | 0.932 |


[^0]:    * The author acknowledges financial support from CAPES and the hospitality of the European University Institute and the CES-University of Munich during different stages of the elaboration of this work.

[^1]:    1 Alternatively, input distance functions would emphasize input conservation. The two orientations are only necessarily equivalent under constant returns to scale. In the present paper I consider the output orientation throughout the comparison exercises across different techniques as the emphasis will be in the degree of structure conferred to the error term. In any case, it is often common that the orientation does not give rise to important differences in terms of the efficiency scores as for example is often the case in applications of Data Envelopment Analysis [see e.g. Berg and Lim (2006)].

[^2]:    ${ }^{2}$ When one considers robustness checks across different SFA approacjes, usually a reasonable consistency emerges [see e.g. Ahmad and Bravo-Ureta (1996)].

[^3]:    ${ }^{3}$ Morrison Paul et al (2000) provides an application along those lines.

[^4]:    ${ }^{4}$ Since the focus of the paper is on the consistency of the efficiency scores associated with different approaches, the intermediate estimation results will not be presented for conciseness. The results, that indicated a good fit, can be provided upon request. The empirical results ere obtained with the softwares DEA-Solver Professional (DEA), Eviews 5.1 (DF-OLS and DF-RE) and Frontier 4.1 by Tim Coelli (DF-SF-TN1. DF-SF-TN2 and DF-SF-TN3)

[^5]:    ${ }^{5}$ For a useful introduction to multivariate statistical methods see Manly (1994).
    ${ }^{6}$ In that case the variances of the principal components would add up to p .

[^6]:    ${ }^{7}$ More recently, the growing adoption of voice over IP procedures is an example of an important structural change that is difficult to control for in efficiency measurement exercises.

